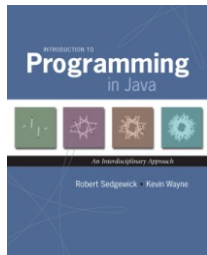
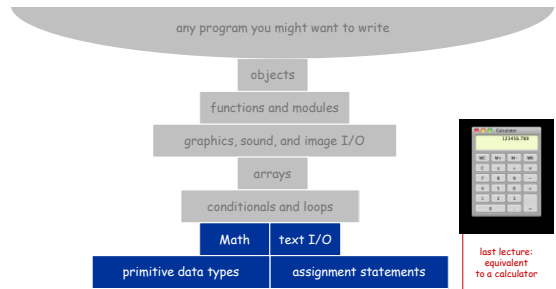


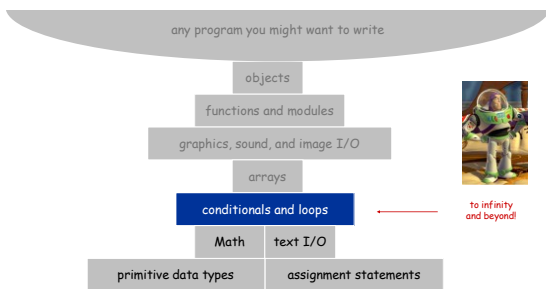
1.3 Conditionals and Loops



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A Foundation for Programming

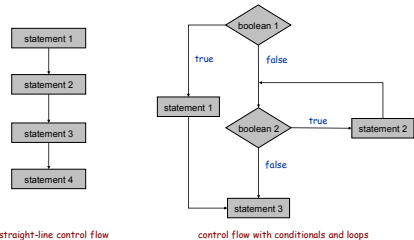


3

Control Flow

Control flow.

- Sequence of statements that are actually executed in a program.
- Conditionals and loops: enable us to choreograph control flow.



4

Conditionals



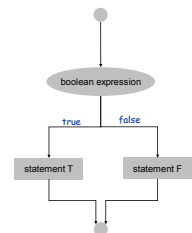
If Statement

The `if` statement. A common branching structure.

- Evaluate a `boolean` expression.
- If `true`, execute some statements.
- If `false`, execute other statements.

```
if (boolean expression) {
    statement T;
}
else {
    statement F;
}
```

can be any sequence of statements

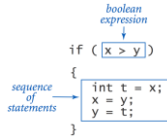


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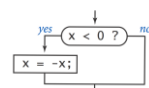
If Statement

The `if` statement. A common branching structure.

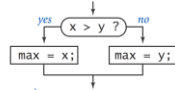
- Evaluate a `boolean` expression.
- If `true`, execute some statements.
- If `false`, execute other statements.



`if (x < 0) x = -x;`



`if (x > y) max = x;`
`else max = y;`



If Statement

Ex. Take different action depending on value of variable.

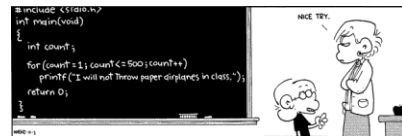
```
public class Flip {
    public static void main(String[] args) {
        if (Math.random() < 0.5) System.out.println("Heads");
        else System.out.println("Tails");
    }
}
```



If Statement Examples

<i>absolute value</i>	<code>if (x < 0) x = -x;</code>
<i>put x and y into sorted order</i>	<code>if (x > y) { int t = x; x = y; y = t; }</code>
<i>maximum of x and y</i>	<code>if (x > y) max = x; else max = y;</code>
<i>error check for division operation</i>	<code>if (den == 0) System.out.println("Division by zero"); else System.out.println("Quotient = " + num/den);</code>
<i>error check for quadratic formula</i>	<code>double discriminant = b*b - 4.0*c; if (discriminant < 0.0) { System.out.println("No real roots"); } else { System.out.println((-b + Math.sqrt(discriminant))/2.0); System.out.println((-b - Math.sqrt(discriminant))/2.0); }</code>

The For Loop

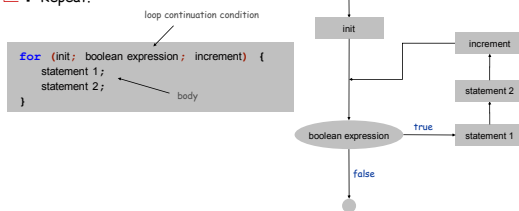


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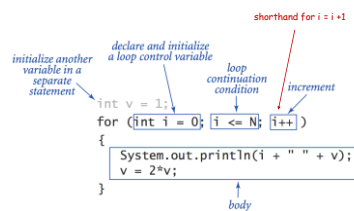
For Loops

The `for` loop. A common repetition structure.

- Execute initialization statement.
- Evaluate a `boolean` expression.
- If `true`, execute some statements.
- And then the increment statement.
- Repeat.



Anatomy of a For Loop



Q. What does it print?

A.

For Loop: Powers of Two

- Ex. Print powers of 2 that are $\leq 2^N$.
- Increment i from 0 to n .
 - Double v each time.

```
int v = 1;
for (int i = 0; i <= N; i++) {
    System.out.println(i + " " + v);
    v = 2 * v;
}
```

i	v	i <= N
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	false

```
0 1
1 2
2 4
3 8
4 16
5 32
6 64
```

N = 6



Click for demo

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For Loops: Subdivisions of a Ruler

Create subdivision of a ruler.

- Initialize ruler to " ".
- For each value i from 1 to n : sandwich two copies of ruler on either side of i .

```
public class RulerN {
    public static void main(String[] args) {
        int N = Integer.parseInt(args[0]);
        String ruler = " ";
        for (int i = 1; i <= N; i++) {
            ruler = ruler + i + ruler;
        }
        System.out.println(ruler);
    }
}
```

i	ruler
	" "
1	" 1 "
2	" 1 2 1 "
3	" 1 2 1 3 1 2 1 "

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For Loops: Subdivisions of a Ruler

```
% java RulerN 1
1

% java RulerN 2
1 2 1

% java RulerN 3
1 2 1 3 1 2 1

% java RulerN 4
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1

% java RulerN 5
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1 5 1 2 1 3 1 2 1 4 1 2 1 3 1 2 1

% java RulerN 100
Exception in thread "main"
java.lang.OutOfMemoryError
```

Observation. Loops can produce a huge amount of output!

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The While Loop



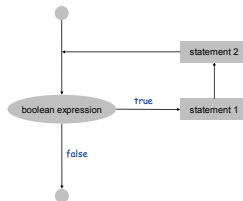
16

While Loop

The while loop. Another common repetition structure.

- Evaluate a boolean expression.
- If true, execute some statements.
- Repeat.

```
while (boolean expression) {
    statement 1;
    statement 2;
}
```



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While Loop: Powers of Two

Ex. Print powers of 2 that are $\leq 2^N$.

- Increment i from 0 to n .
- Double v each time.

```
int i = 0;
int v = 1;
while (i <= N) {
    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
}
```

i	v	i <= N
0	1	true
1	2	true
2	4	true
3	8	true
4	16	true
5	32	true
6	64	true
7	128	false

```
0 1
1 2
2 4
3 8
4 16
5 32
6 64
```

N = 6



Click for demo

18

Powers of Two

```
public class PowersOfTwo {
    public static void main(String[] args) {
        // last power of two to print
        int N = Integer.parseInt(args[0]);

        int i = 0; // loop control counter
        int v = 1; // current power of two
        while (i <= N) {
            System.out.println(i + " " + v);
            i = i + 1;
            v = 2 * v;
        }
    }
}
```

```
% java PowersOfTwo 3
0 1
1 2
2 4
3 8

% java PowersOfTwo 6
0 1
1 2
2 4
3 8
4 16
5 32
6 64
```

19

While Loop Challenge

Q. Anything wrong with the following code for printing powers of 2?

```
int i = 0;
int v = 1;
while (i < N)
    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
```

20

While Loop Challenge

Q. Anything wrong with the following code for printing powers of 2?

```
int i = 0;
int v = 1;
while (i <= N)
    System.out.println(i + " " + v);
    i = i + 1;
    v = 2 * v;
```

A. Need curly braces around statements in while loop; otherwise it enters an infinite loop, printing "0 1".

Moment of panic. How to stop infinite loop?

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While Loops: Square Root

Goal. Implement `Math.sqrt()`.

```
% java Sqrt 2.0
1.414213562373095
```

Newton-Raphson method to compute the square root of c :

- Initialize $t_0 = c$.
- Repeat until $t_i = c / t_i$, up to desired precision: set t_{i+1} to be the average of t_i and c / t_i .

15 decimal digits of accuracy in 5 iterations

t_0	=	2.0
t_1	=	$\frac{1}{2}(t_0 + \frac{c}{t_0}) = 1.5$
t_2	=	$\frac{1}{2}(t_1 + \frac{c}{t_1}) = 1.4166666666666665$
t_3	=	$\frac{1}{2}(t_2 + \frac{c}{t_2}) = 1.4142156862745097$
t_4	=	$\frac{1}{2}(t_3 + \frac{c}{t_3}) = 1.4142135623746899$
t_5	=	$\frac{1}{2}(t_4 + \frac{c}{t_4}) = 1.414213562373095$

computing the square root of 2



"A wonderful square root. Let's hope it can be used for the good of mankind!"

Copyright 2004, Sidney Harris
www.cartoonists.com

22

While Loops: Square Root

Goal. Implement `Math.sqrt()`.

```
% java Sqrt 2.0
1.414213562373095
```

Newton-Raphson method to compute the square root of c :

- Initialize $t_0 = c$.
- Repeat until $t_i = c / t_i$, up to desired precision: set t_{i+1} to be the average of t_i and c / t_i .

15 decimal digits of accuracy in 5 iterations

```
public class Sqrt {
    public static void main(String[] args) {
        double epsilon = 1e-15;
        double c = Double.parseDouble(args[0]);
        double t = c;
        while (Math.abs(t - c/t) > t*epsilon) {
            t = (c/t + t) / 2.0;
        }
        System.out.println(t);
    }
}
```

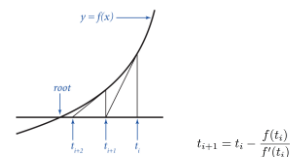
relative error tolerance

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Newton-Raphson Method

Square root method explained.

- Goal: find root of any function $f(x)$.
- Start with estimate t_0 .
- Draw line tangent to curve at $x = t_i$.
- Set t_{i+1} to be x -coordinate where line hits x -axis.
- Repeat until desired precision.



Technical conditions. $f(x)$ is smooth; t_0 is good estimate.

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Loop Examples

<i>print largest power of two less than or equal to N</i>	<pre>int v = 1; while (v <= N/2) v = 2*v; System.out.println(v);</pre>
<i>compute a finite sum (1 + 2 + ... + N)</i>	<pre>int sum = 0; for (int i = 1; i <= N; i++) sum += i; System.out.println(sum);</pre>
<i>compute a finite product (N! = 1 × 2 × ... × N)</i>	<pre>int product = 1; for (int i = 1; i <= N; i++) product *= i; System.out.println(product);</pre>
<i>print a table of function values</i>	<pre>for (int i = 0; i <= N; i++) System.out.println(i + " " + 2*Math.PI*i/N);</pre>

Nesting



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Nested If Statements

Ex. Pay a certain tax rate depending on income level.

Income	Rate
0 - 47,450	22%
47,450 - 114,650	25%
114,650 - 174,700	28%
174,700 - 311,950	33%
311,950 -	35%

5 mutually exclusive alternatives

```
double rate;
if (income < 47450) rate = 0.22;
else if (income < 114650) rate = 0.25;
else if (income < 174700) rate = 0.28;
else if (income < 311950) rate = 0.33;
else rate = 0.35;
```

graduated income tax calculation

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Nested If Statements

Use **nested if** statements to handle multiple alternatives.

```
if (income < 47450) rate = 0.22;
else {
    if (income < 114650) rate = 0.25;
    else {
        if (income < 174700) rate = 0.28;
        else {
            if (income < 311950) rate = 0.33;
            else rate = 0.35;
        }
    }
}
```

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Nested If Statements

Need all those braces? Not always.

```
if (income < 47450) rate = 0.22;
else if (income < 114650) rate = 0.25;
else if (income < 174700) rate = 0.28;
else if (income < 311950) rate = 0.33;
else rate = 0.35;
```

is shorthand for

```
if (income < 47450) rate = 0.22;
else {
    if (income < 114650) rate = 0.25;
    else {
        if (income < 174700) rate = 0.28;
        else {
            if (income < 311950) rate = 0.33;
            else rate = 0.35;
        }
    }
}
```

but **be careful** when nesting if-else statements. [See Q+A on p. 75.]

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Nested If Statement Challenge

Q. What's wrong with the following for income tax calculation?

Income	Rate
0 - 47,450	22%
47,450 - 114,650	25%
114,650 - 174,700	28%
174,700 - 311,950	33%
311,950 -	35%

```
double rate = 0.35;
if (income < 47450) rate = 0.22;
if (income < 114650) rate = 0.25;
if (income < 174700) rate = 0.28;
if (income < 311950) rate = 0.33;
```

wrong graduated income tax calculation

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Monte Carlo Simulation



Gambler's ruin. Gambler starts with \$stake and places \$1 fair bets until going broke or reaching \$goal.

- What are the chances of winning?
- How many bets will it take?

One approach. Monte Carlo simulation.

- Flip digital coins and see what happens.
- Repeat and compute statistics.



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Gambler's Ruin

```
public class Gambler {
    public static void main(String[] args) {
        int stake = Integer.parseInt(args[0]);
        int goal = Integer.parseInt(args[1]);
        int T = Integer.parseInt(args[2]);
        int wins = 0;

        // repeat experiment T times
        for (int t = 0; t < T; t++) {

            // do one gambler's ruin experiment
            int cash = stake;
            while (cash > 0 && cash < goal) {

                // flip coin and update
                if (Math.random() < 0.5) cash++;
                else cash--;

            }
            if (cash == goal) wins++;

        }
        System.out.println(wins + " wins of " + T);
    }
}
```

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Digression: Simulation and Analysis

```
stake goal T
// // //
% java Gambler 5 25 1000
191 wins of 1000
% java Gambler 5 25 1000
203 wins of 1000
% java Gambler 500 2500 1000
197 wins of 1000
```

after a substantial wait...

Fact. Probability of winning = stake ÷ goal.

Fact. Expected number of bets = stake × desired gain.

Ex. 20% chance of turning \$500 into \$2500,

but expect to make one million \$1 bets.

$$500/2500 = 20\%$$

$$500 * (2500 - 500) = 1 \text{ million}$$

Remark. Both facts can be proved mathematically; for more complex scenarios, computer simulation is often the best (only) plan of attack.

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Control Flow Summary

Control flow.

- Sequence of statements that are actually executed in a program.
- Conditionals and loops: enable us to choreograph the control flow.

Extra Slides

Control Flow	Description	Examples
straight-line programs	all statements are executed in the order given	
conditionals	certain statements are executed depending on the values of certain variables	if if-else
loops	certain statements are executed repeatedly until certain conditions are met	while for do-while

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Oblivious Sorting

Sort. Read in 3 integers and rearrange them in ascending order.

```
public class Sort3 {
    public static void main(String[] args) {
        int a = Integer.parseInt(args[0]);
        int b = Integer.parseInt(args[1]);
        int c = Integer.parseInt(args[2]);

        if (b > c) { int t = b; b = c; c = t; }
        if (a > b) { int t = a; a = b; b = t; }
        if (b > c) { int t = b; b = c; c = t; }

        System.out.println(a + " " + b + " " + c);
    }
}
```

read in 3 integers from command-line

swap b and c

swap a and b

swap b and c

```
% java Sort3 9 8 7
7 8 9
% java Sort3 2 1 7
1 2 7
```

- Puzzle 1. Sort 4 integers with 5 compare-exchanges.
- Puzzle 2. Sort 6 integers with 12.

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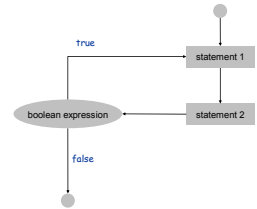
Do-While Loop

The **do-while** loop. A less common repetition structure.

- Execute sequence of statements.
- Check loop-continuation condition.
- Repeat.

```
do {
    statement 1;
    statement 2;
} while (boolean expression);
```

do-while loop syntax



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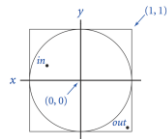
Do-While Loop

Ex. Find a point (x, y) that is uniformly distributed in unit disc.

- Pick a random point in unit square.
- Check if point is also in unit disc.
- Repeat.

```
do {
    x = 2.0 * Math.random() - 1.0;
    y = 2.0 * Math.random() - 1.0;
} while (x*x + y*y > 1.0);
```

between -1 and 1



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