

Programming Languages and Techniques (CIS120)

Lecture 17

Hidden State, Objects

Chapter 17

Announcements

- Homework 5: GUI Programming
 - Available soon
 - Due: Oct 22nd
- Fall Break:
 - No lab/recitation sections this week
 - No class on Friday

Hidden State

Encapsulating State

An “incr” function

- Functions with internal state

```
type counter_state = { mutable count:int }
```

```
let ctr = { count = 0 }
```

```
(* each call to incr will produce the next integer *)
```

```
let incr () : int =  
  ctr.count <- ctr.count + 1;  
  ctr.count
```

- Drawbacks:
 - *No modularity*: There is only one counter in the world. If we want another counter, we need to build another counter_state value (say, ctr2) and another incrementing function (incr2)
 - *No encapsulation*: Code anywhere in the rest of the program can modify count

Using Hidden State

- Better: Make a function that creates a counter state and an incr function each time a counter is needed

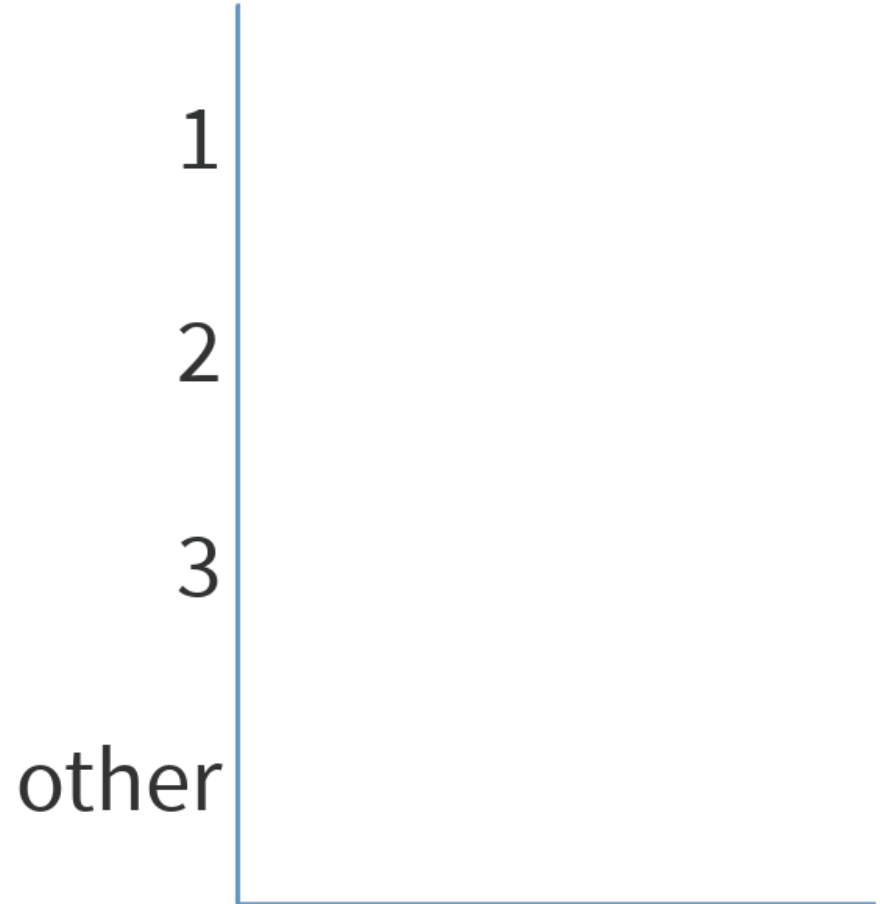
```
(* More useful: a counter generator: *)  
let mk_incr () : unit -> int =  
  (* this ctr is private to the returned function *)  
  let ctr = { count = 0 } in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

```
(* make one counter *)  
let incr1 : unit -> int = mk_incr ()
```

```
(* make another counter *)  
let incr2 : unit -> int = mk_incr ()
```

What number is printed by this program?

```
let mk_incr () : unit -> int =  
  let ctr = { count = 0 } in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count  
  
let incr1 = mk_incr () (* make one counter *)  
let incr2 = mk_incr () (* and another *)  
  
let _ = incr1 () in print_int (incr2 ())
```



What number is printed by this program?

```
let mk_incr () : unit -> int =  
  let ctr = { count = 0 } in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count  
  
let incr1 = mk_incr () (* make one counter *)  
let incr2 = mk_incr () (* and another *)  
  
let _ = incr1 () in print_int (incr2 ())
```

1. 1
2. 2
3. 3
4. other



What is your current level of comfort with the Abstract Stack Machine?

got it well under control

OK but need to work with it a little more

a little puzzled

very puzzled

very very puzzled :-)

Running mk_incr

Workspace

```
let mk_incr () : unit -> int =  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

```
let incr1 : unit -> int =  
mk_incr ()
```

Stack

Heap

Running mk_incr

Workspace

```
let mk_incr : unit -> unit ->  
int = fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

```
let incr1 : unit -> int =  
mk_incr ()
```

Stack

Heap

Running mk_incr

Workspace

```
let mk_incr : unit -> unit ->  
int = fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

```
let incr1 : unit -> int =  
mk_incr ()
```

Stack

Heap

Running mk_incr

Workspace

```
let mk_incr : unit -> unit ->  
int =  
  
let incr1 : unit -> int =  
mk_incr ()
```

Stack

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```


Running mk_incr

Workspace

```
let mk_incr : unit -> unit ->  
int = .  
  
let incr1 : unit -> int =  
mk_incr ()
```

Stack

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```


Running mk_incr

Workspace

```
let incr1 : unit -> int =  
mk_incr ()
```

Stack

mk_incr



Heap

```
fun () ->  
  let ctr = {count = 0} in  
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    ctr.count <- ctr.count + 1;  
    ctr.count
```


Running mk_incr

Workspace

```
let incr1 : unit -> int =  
mk_incr ()
```

Stack

mk_incr



Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

Running mk_incr

Workspace

```
let incr1 : unit -> int =  
( () )
```

Stack

mk_incr

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

Running mk_incr

Workspace

```
let incr1 : unit -> int =  
  (λ ())
```

Stack

mk_incr

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
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Running mk_incr

Workspace

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let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

Stack

mk_incr

```
let incr1 : unit -> int =  
  (___)
```

Heap

```
fun () ->  
  let ctr = {count = 0} in  
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    ctr.count <- ctr.count + 1;  
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Running mk_incr

Workspace

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    ctr.count <- ctr.count + 1;  
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Stack

mk_incr

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Heap

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fun () ->  
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    ctr.count
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Running mk_incr

Workspace

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let ctr = in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

Stack

mk_incr

```
let incr1 : unit -> int =  
(__)
```

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

count 0

Running mk_incr

Workspace

```
let ctr = in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

Stack

mk_incr

```
let incr1 : unit -> int =  
(__)
```

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

count 0

Running mk_incr

Workspace

```
fun () ->  
  ctr.count <- ctr.count + 1;  
  ctr.count
```

Stack

mk_incr

```
let incr1 : unit -> int =  
  (___)
```

ctr

Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

count 0

Running mk_incr

Workspace

```
fun () ->  
  ctr.count <- ctr.count + 1;  
  ctr.count
```

Stack

mk_incr

```
let incr1 : unit -> int =  
  (___)
```

ctr

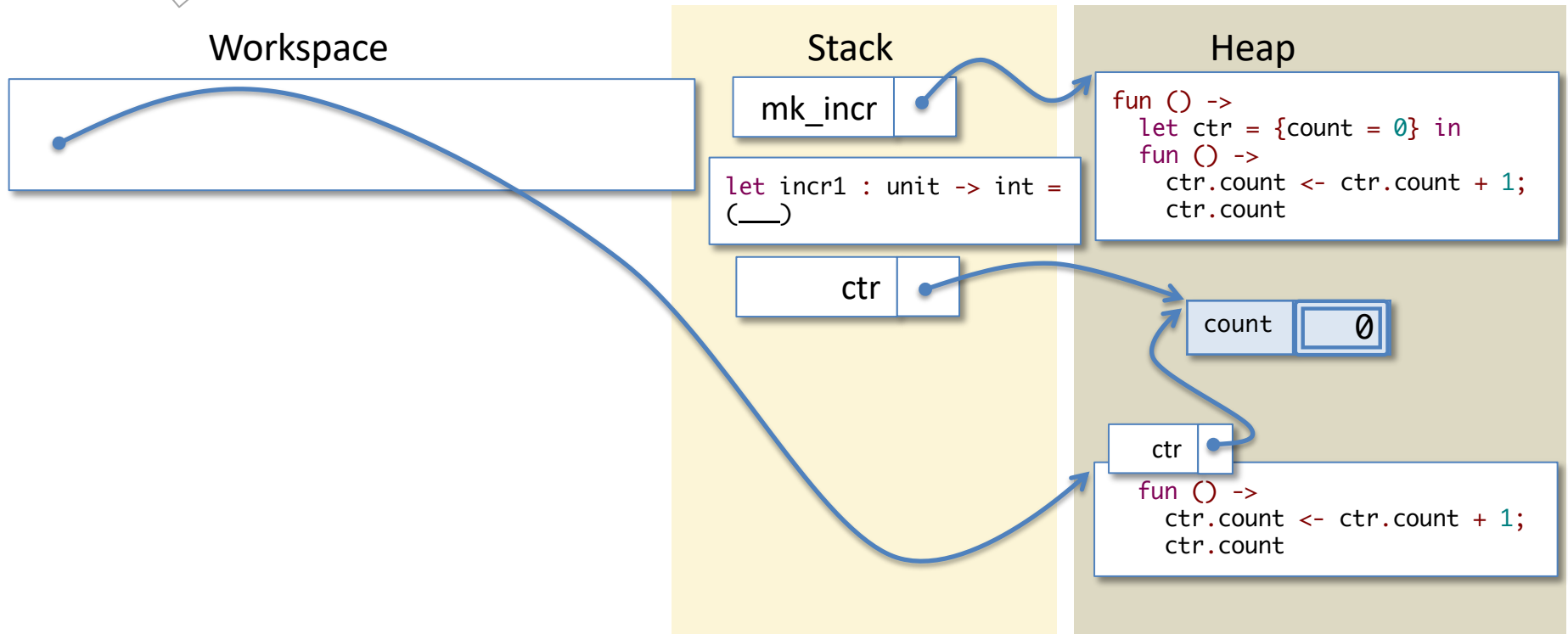
Heap

```
fun () ->  
  let ctr = {count = 0} in  
  fun () ->  
    ctr.count <- ctr.count + 1;  
    ctr.count
```

count 0

Key step!

Local Functions



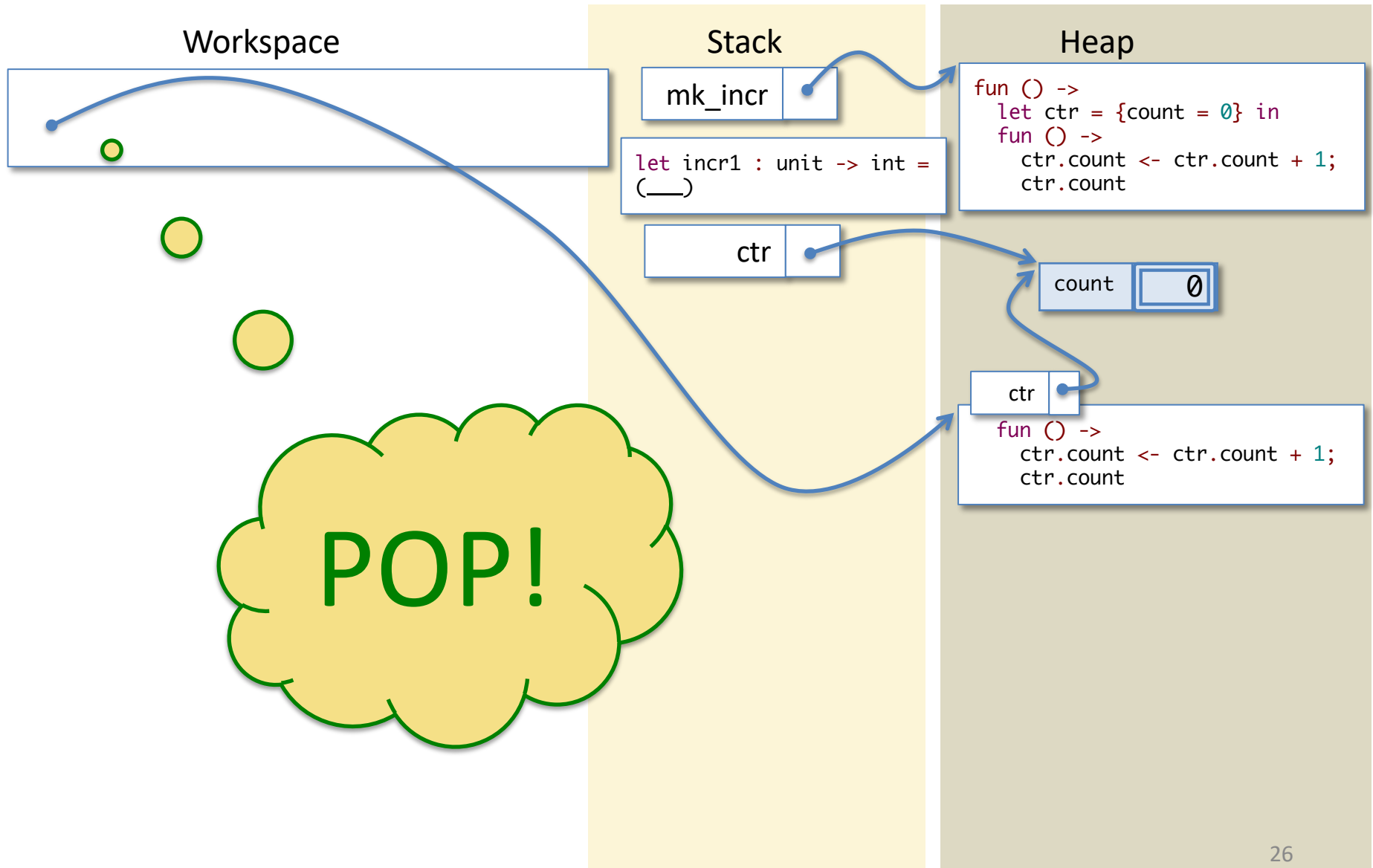
Note: We need one refinement of the ASM model that we've explained so far. Why?

The function body mentions "ctr", which is on the stack at the moment *but about to be popped off...*

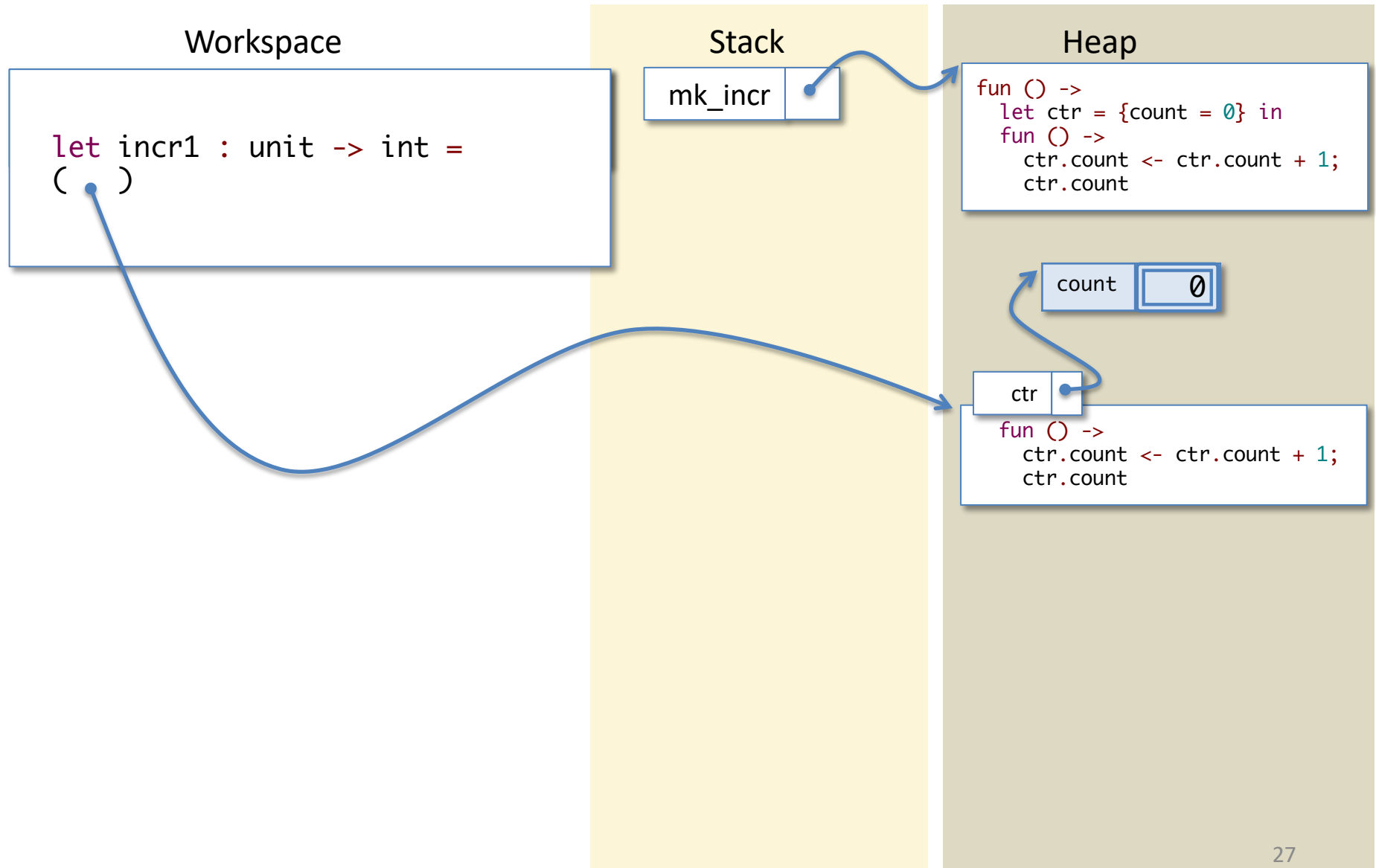
...so we save a copy of the needed stack bindings with the function itself.

This package of "function body plus needed bindings" is called a *closure*...

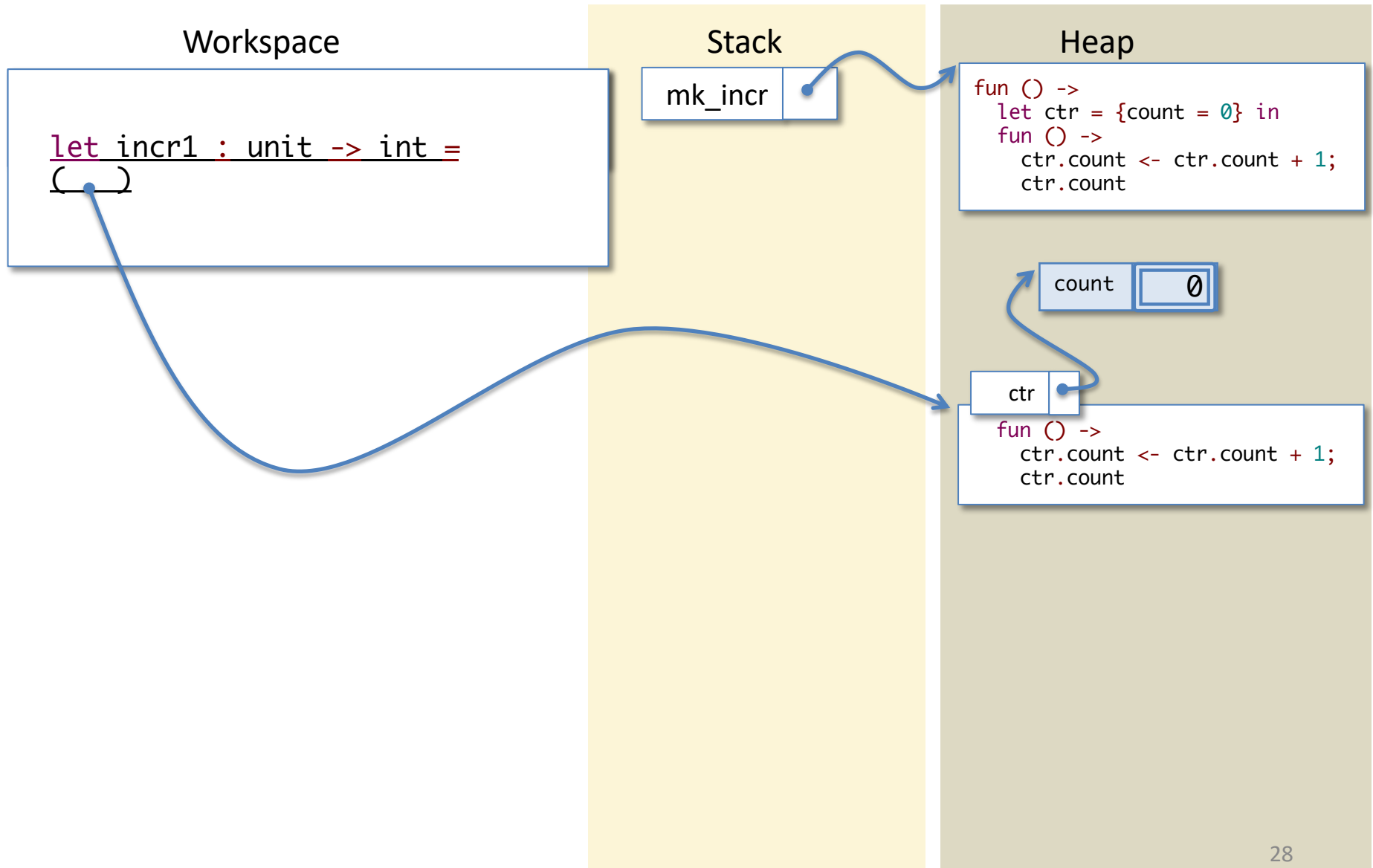
Local Functions



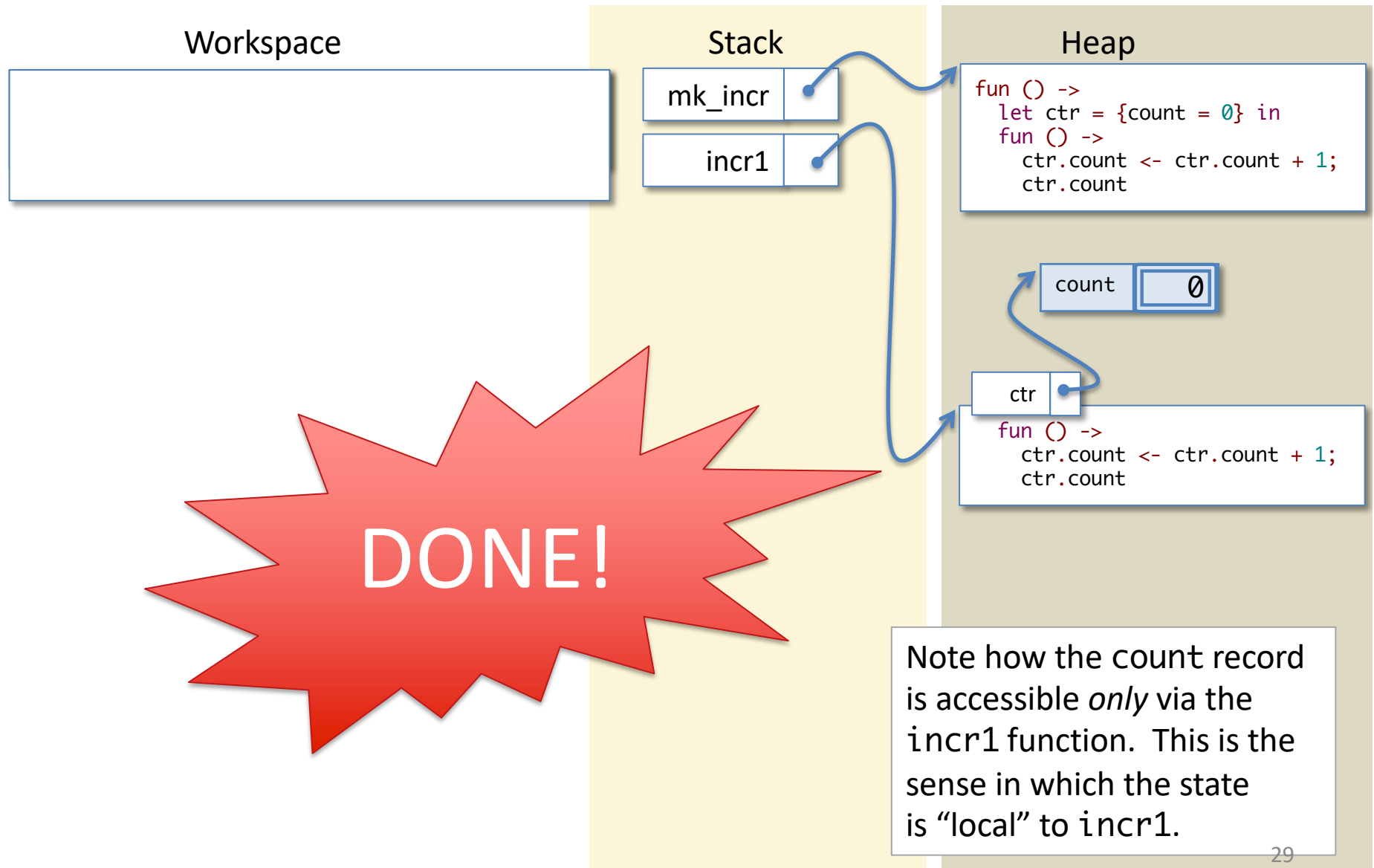
Local Functions



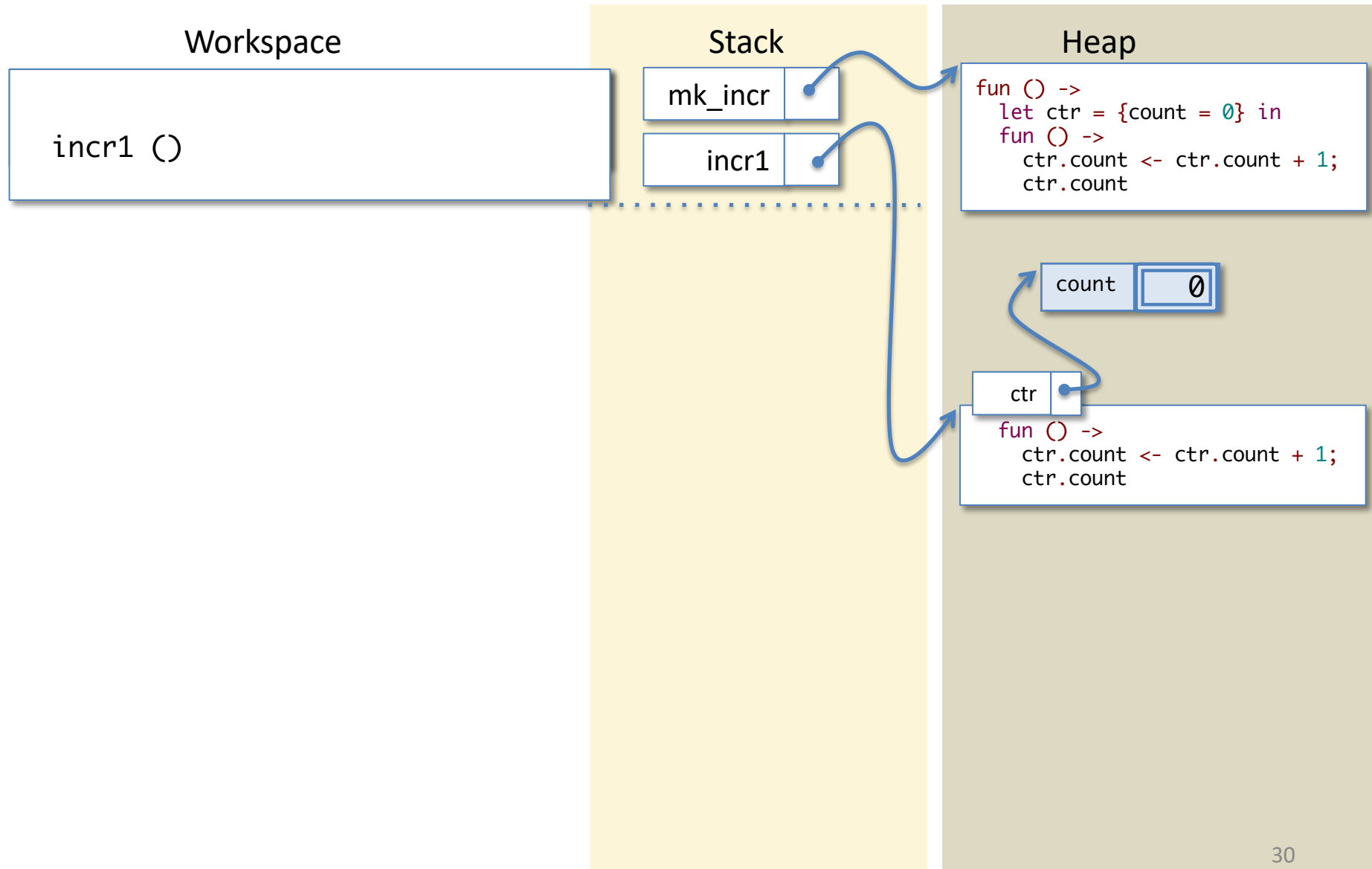
Local Functions



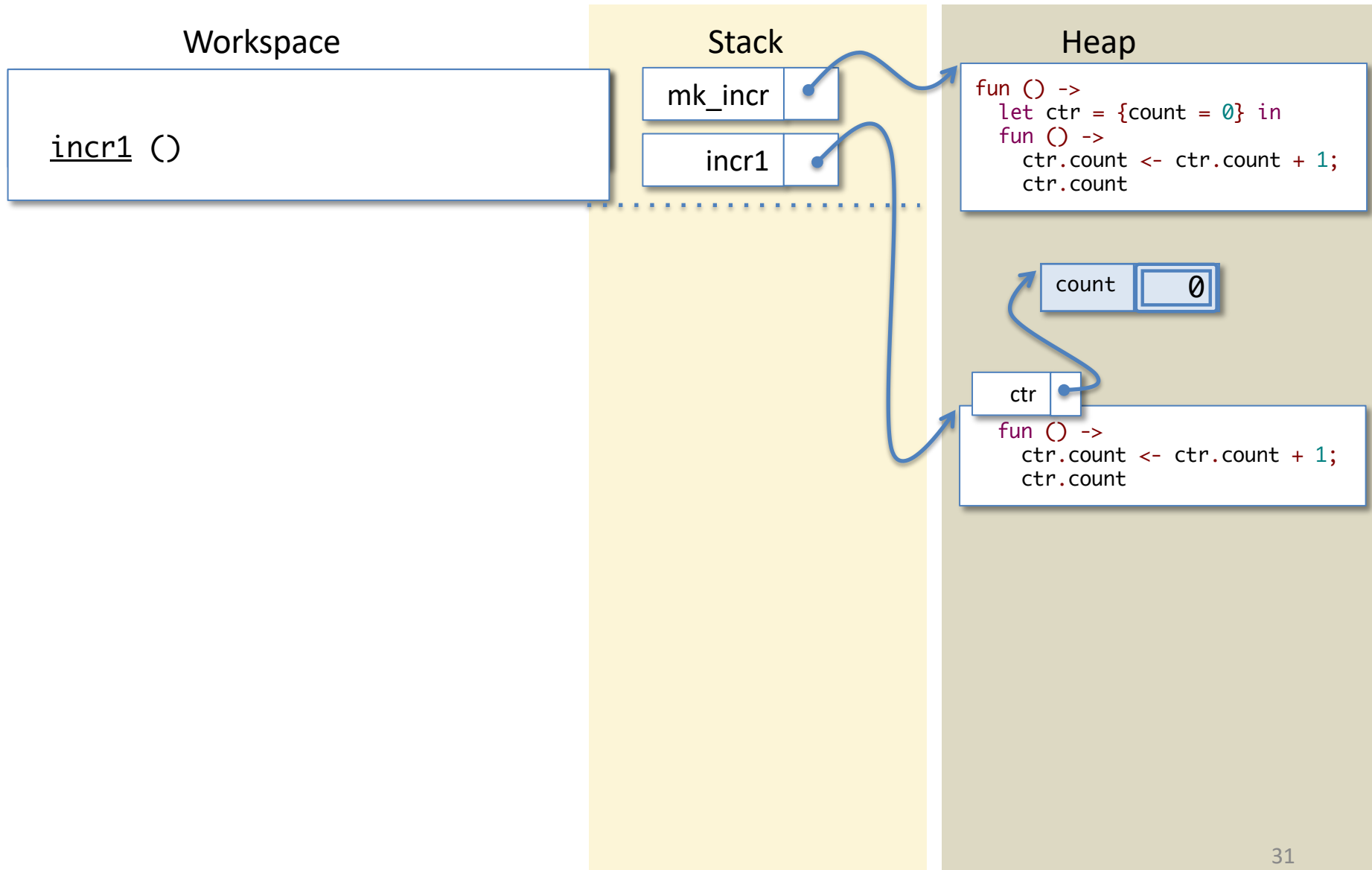
Local Functions



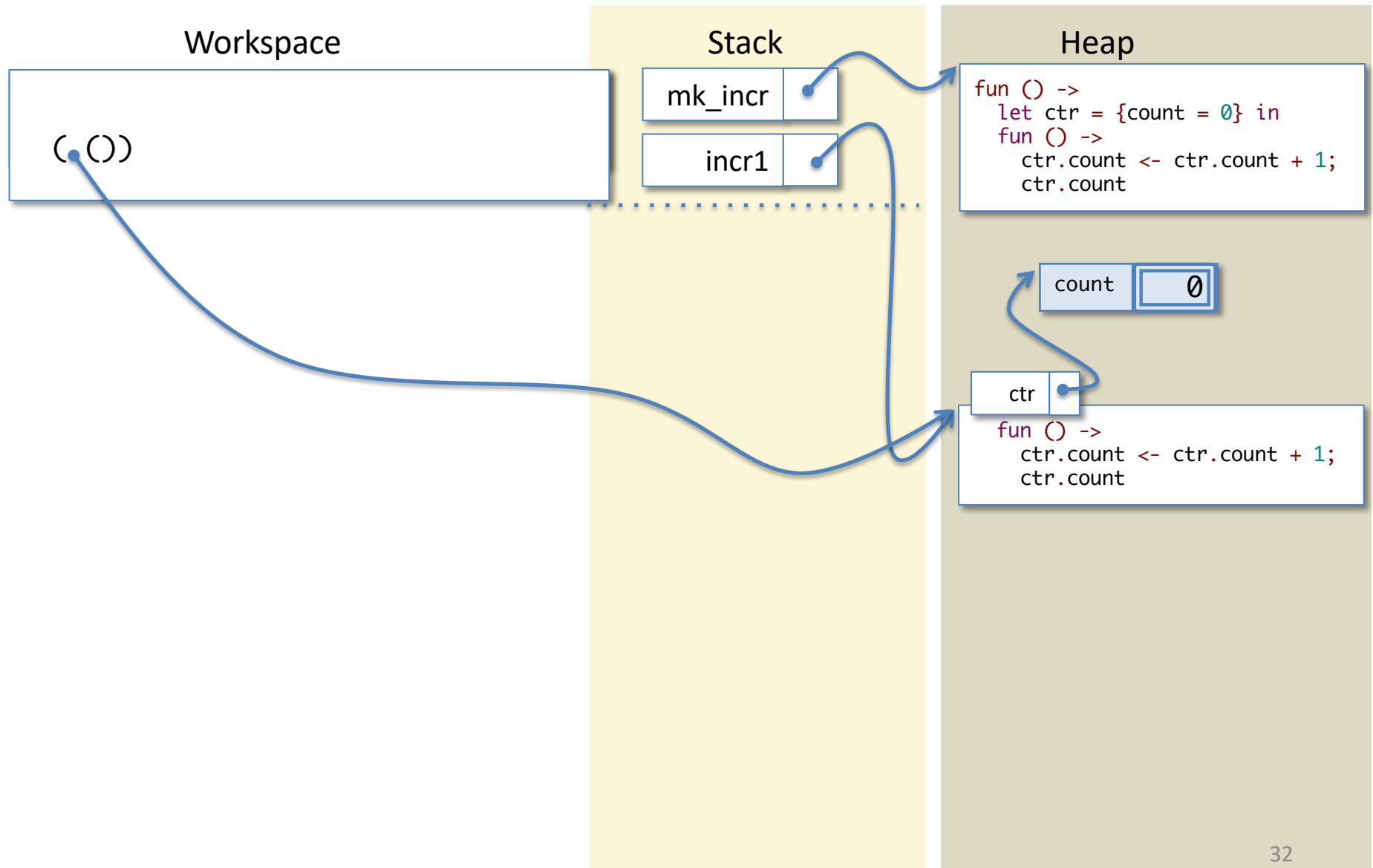
Now let's run "incr1 ()"



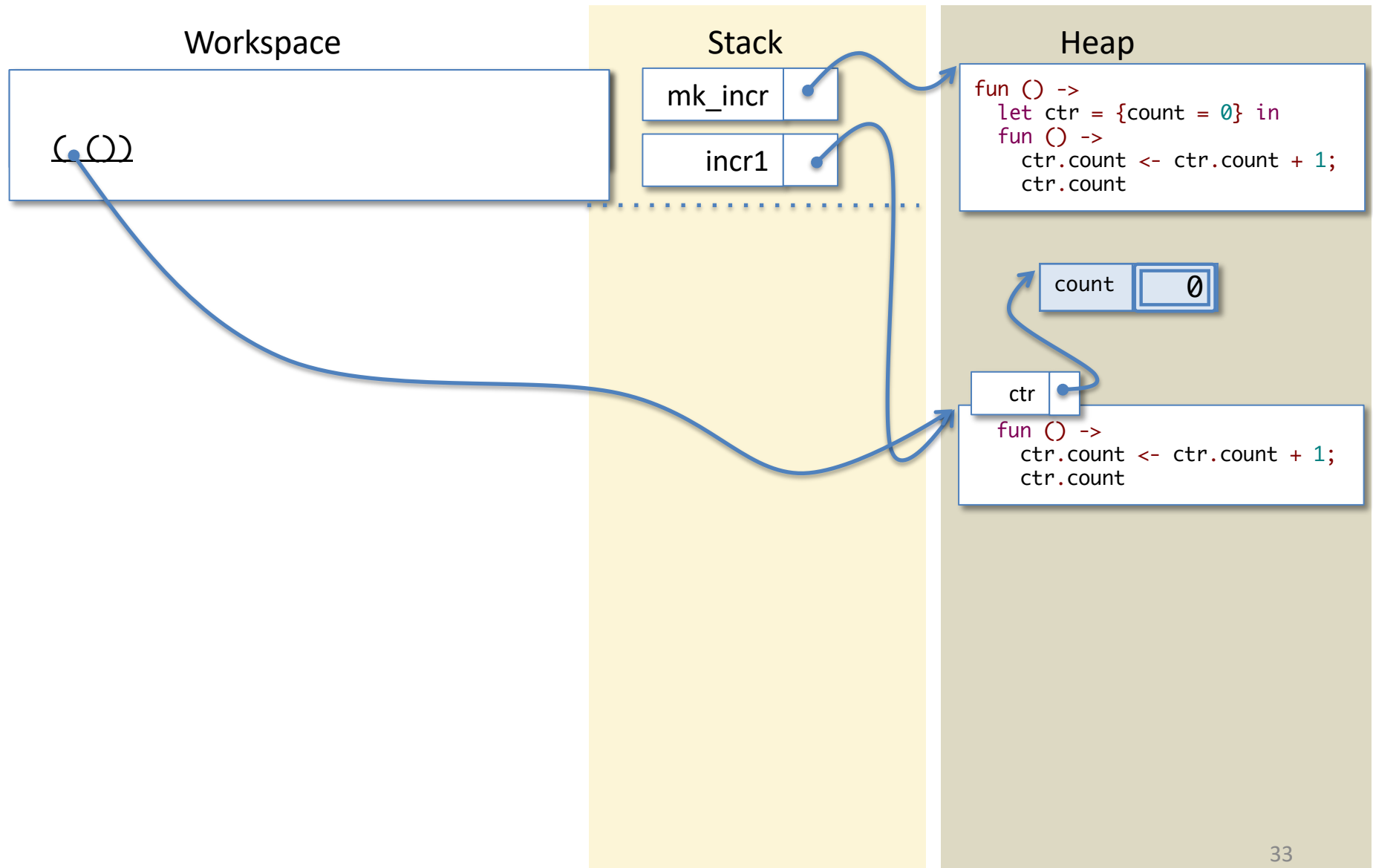
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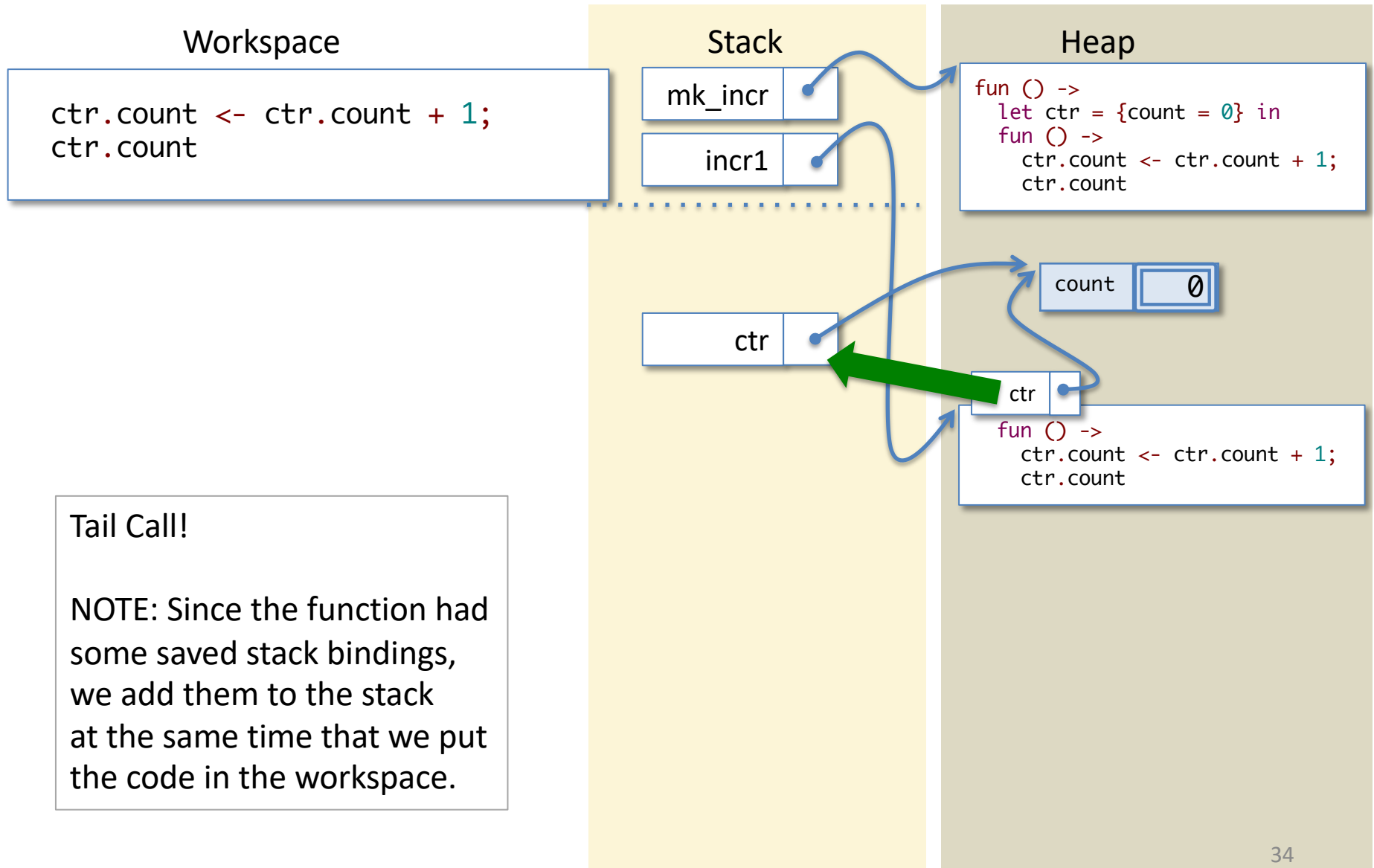
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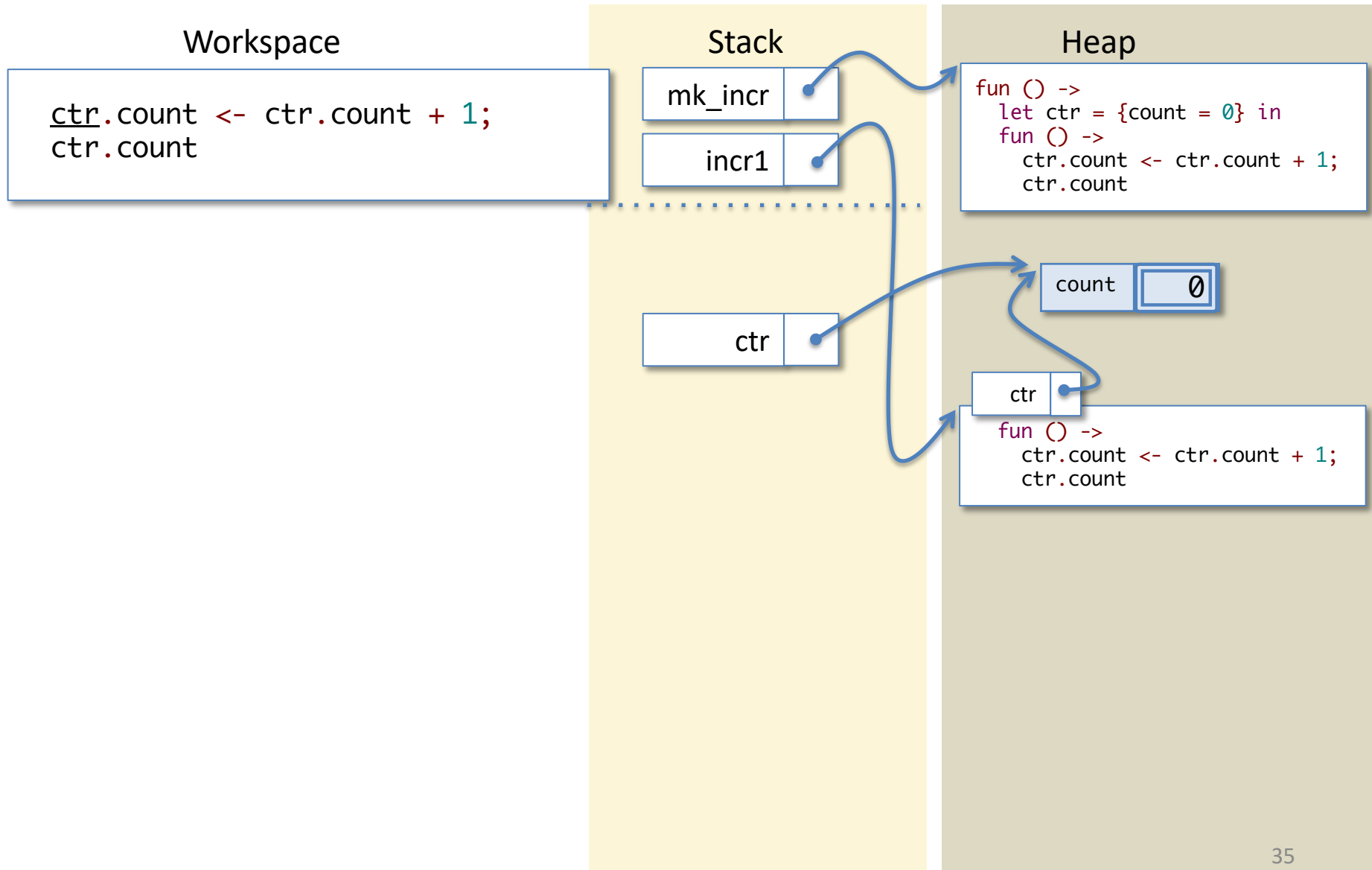
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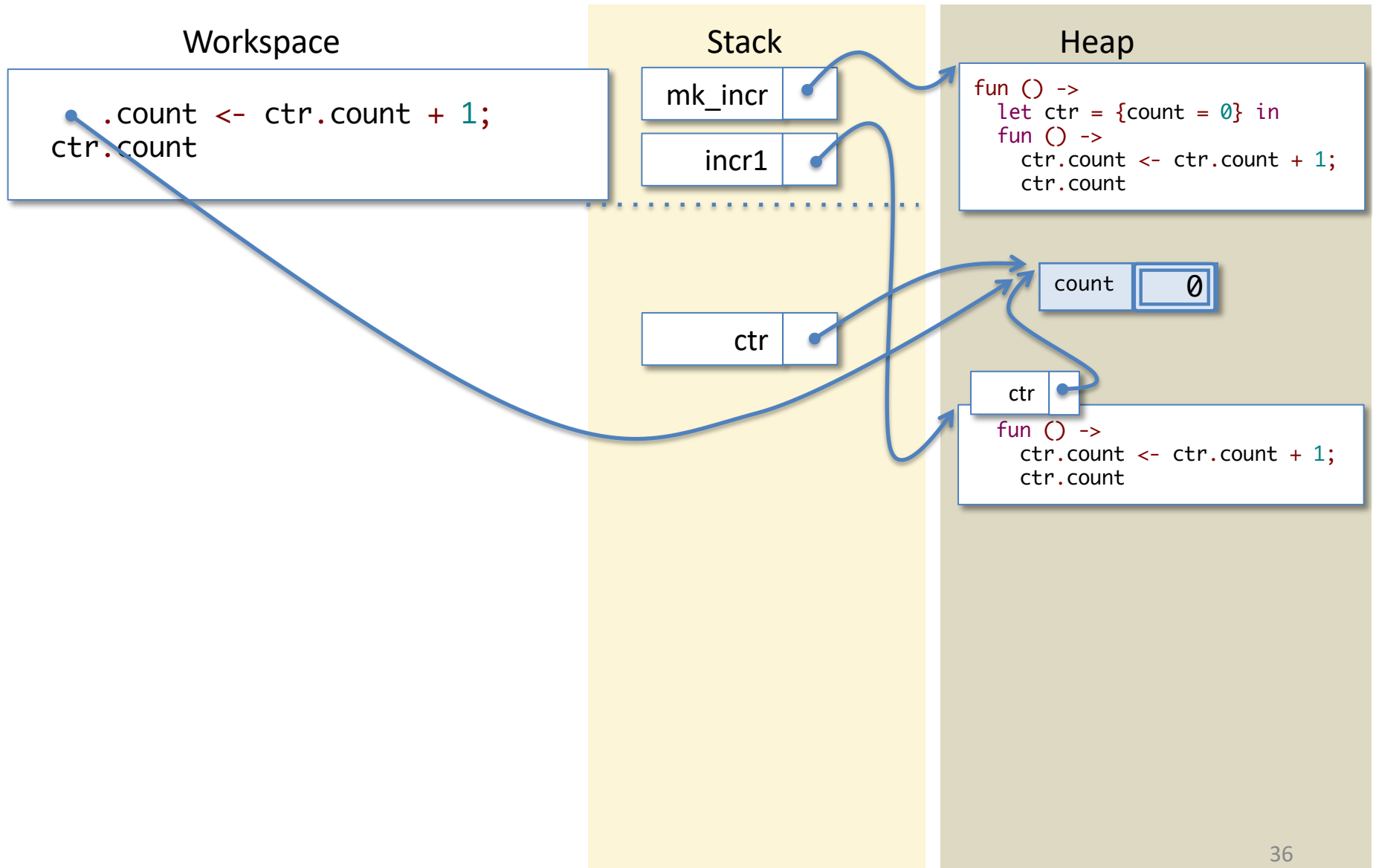
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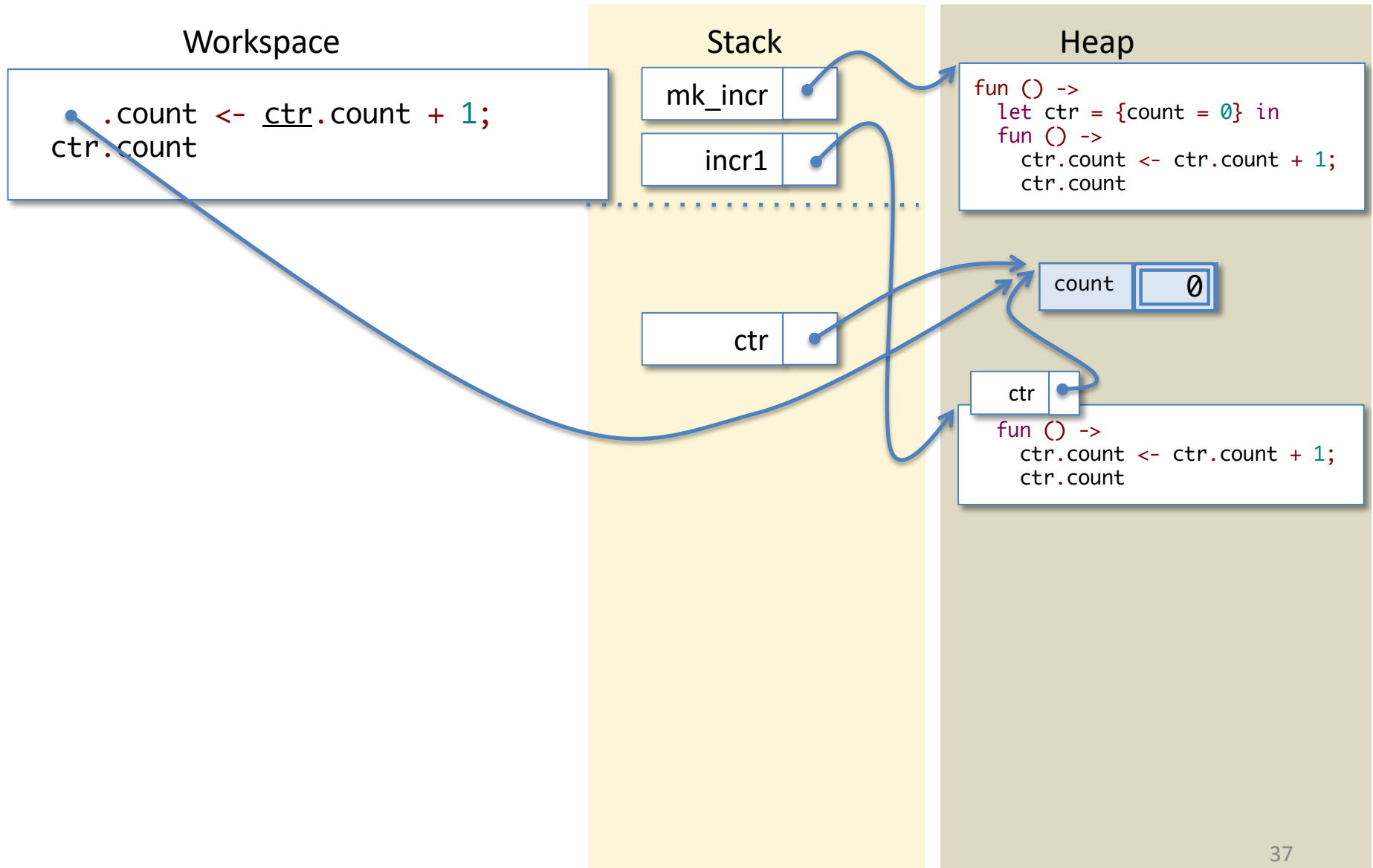
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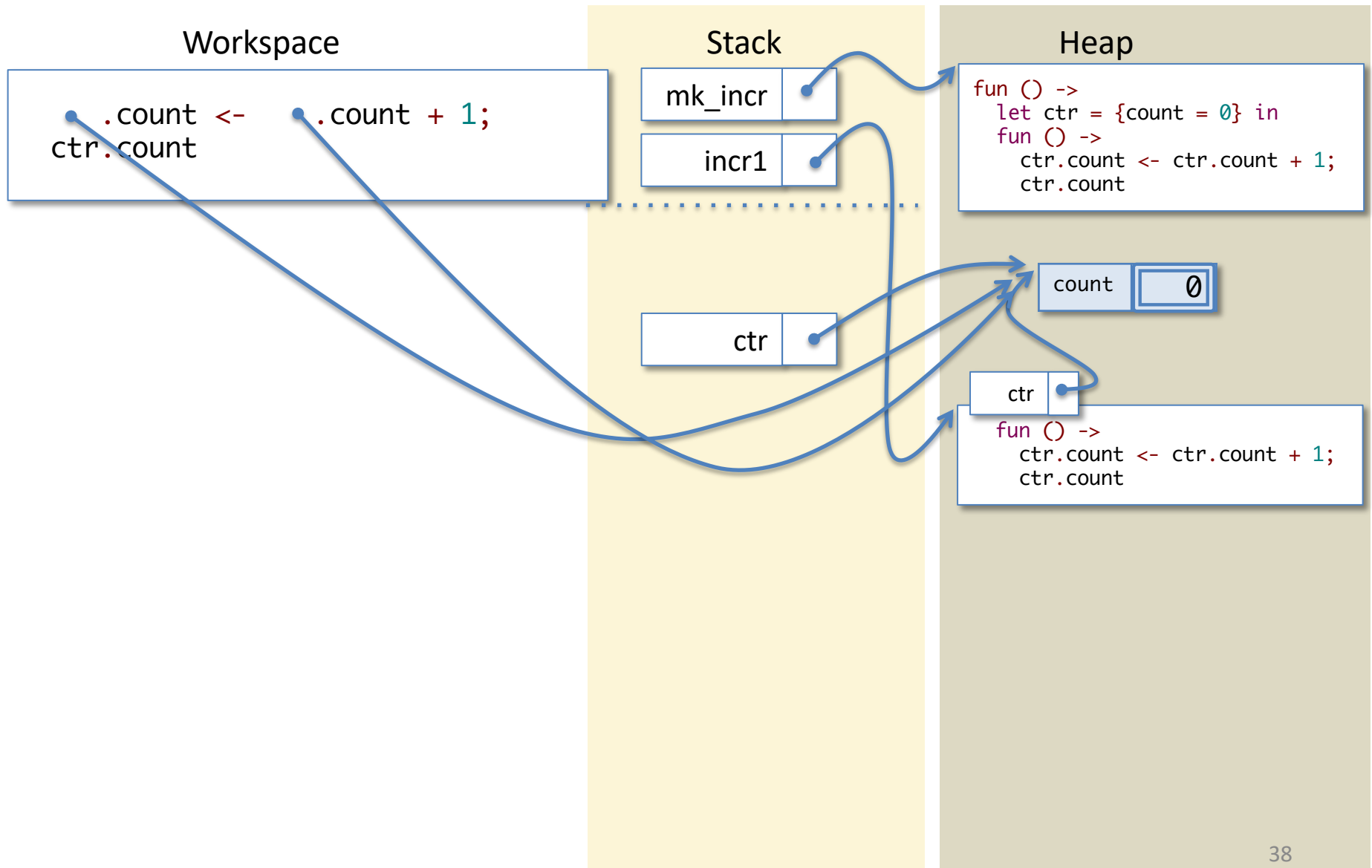
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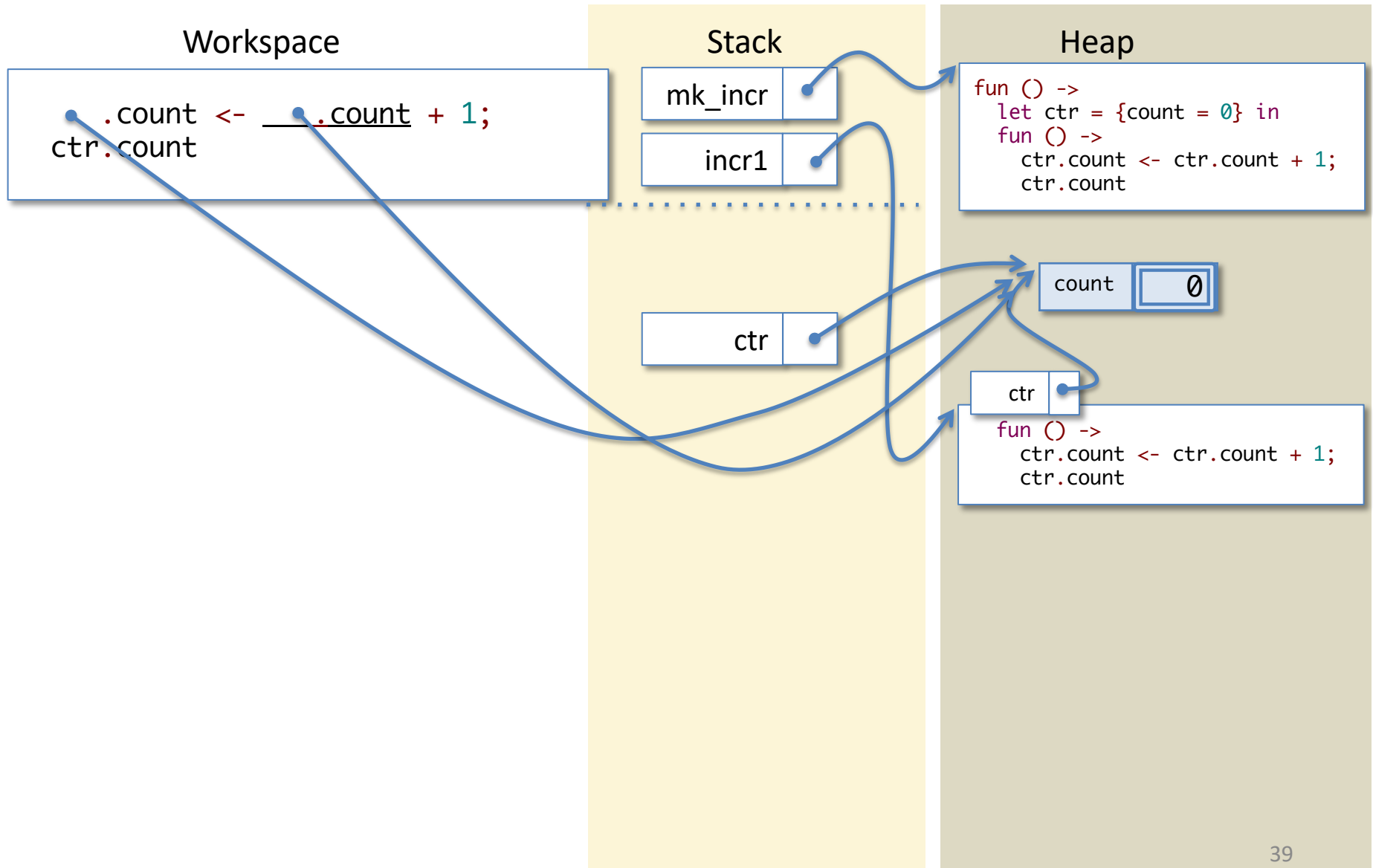
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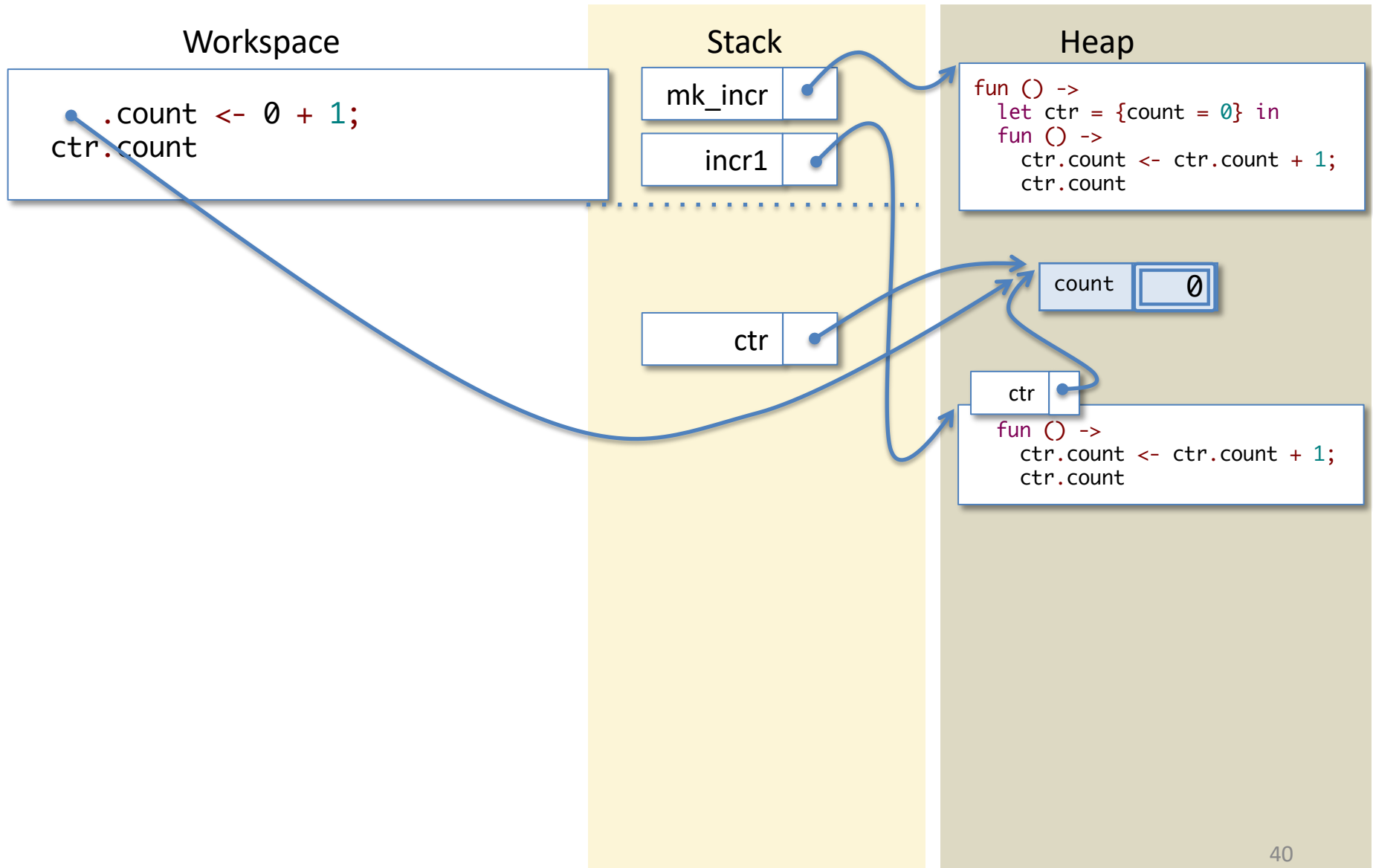
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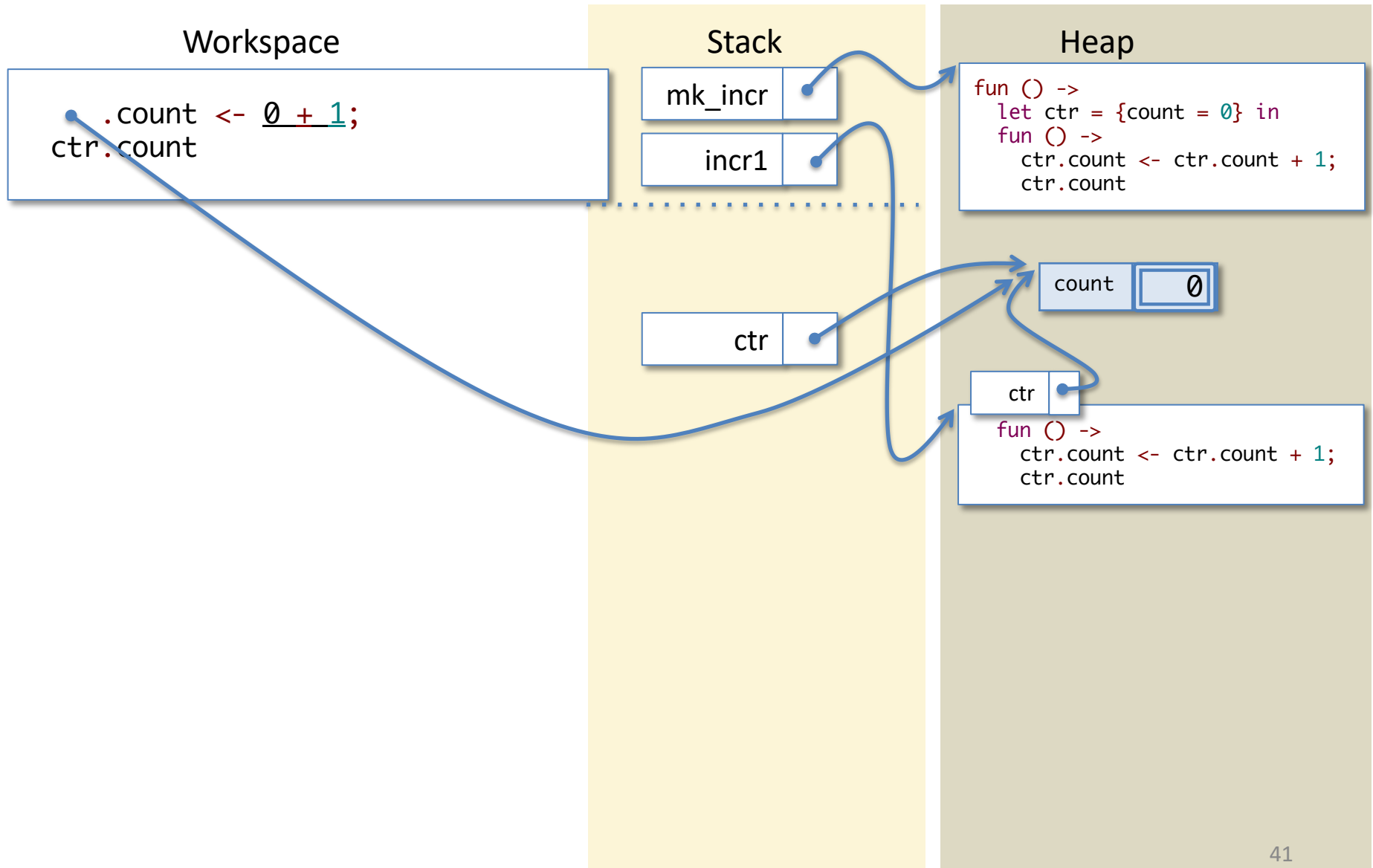
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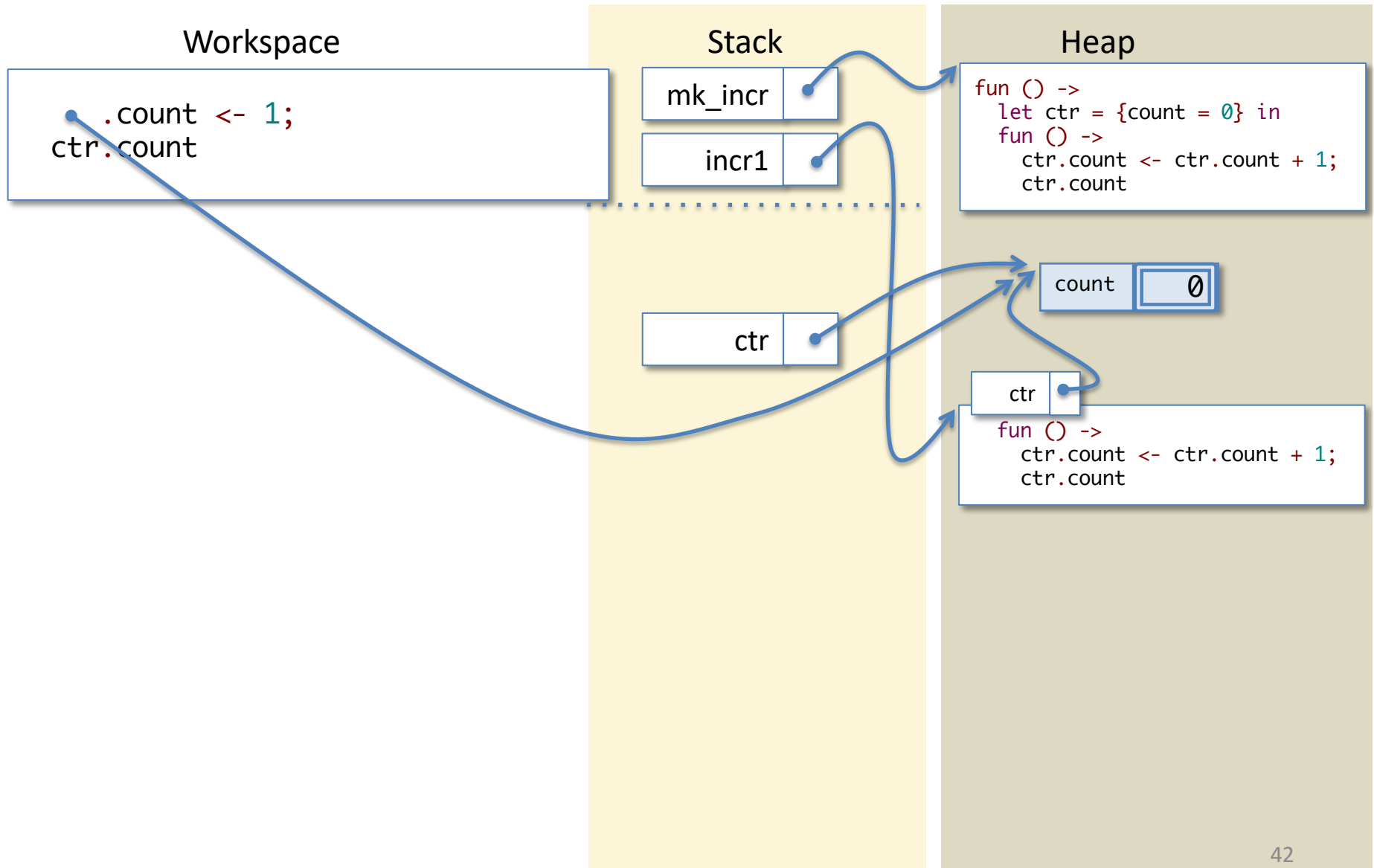
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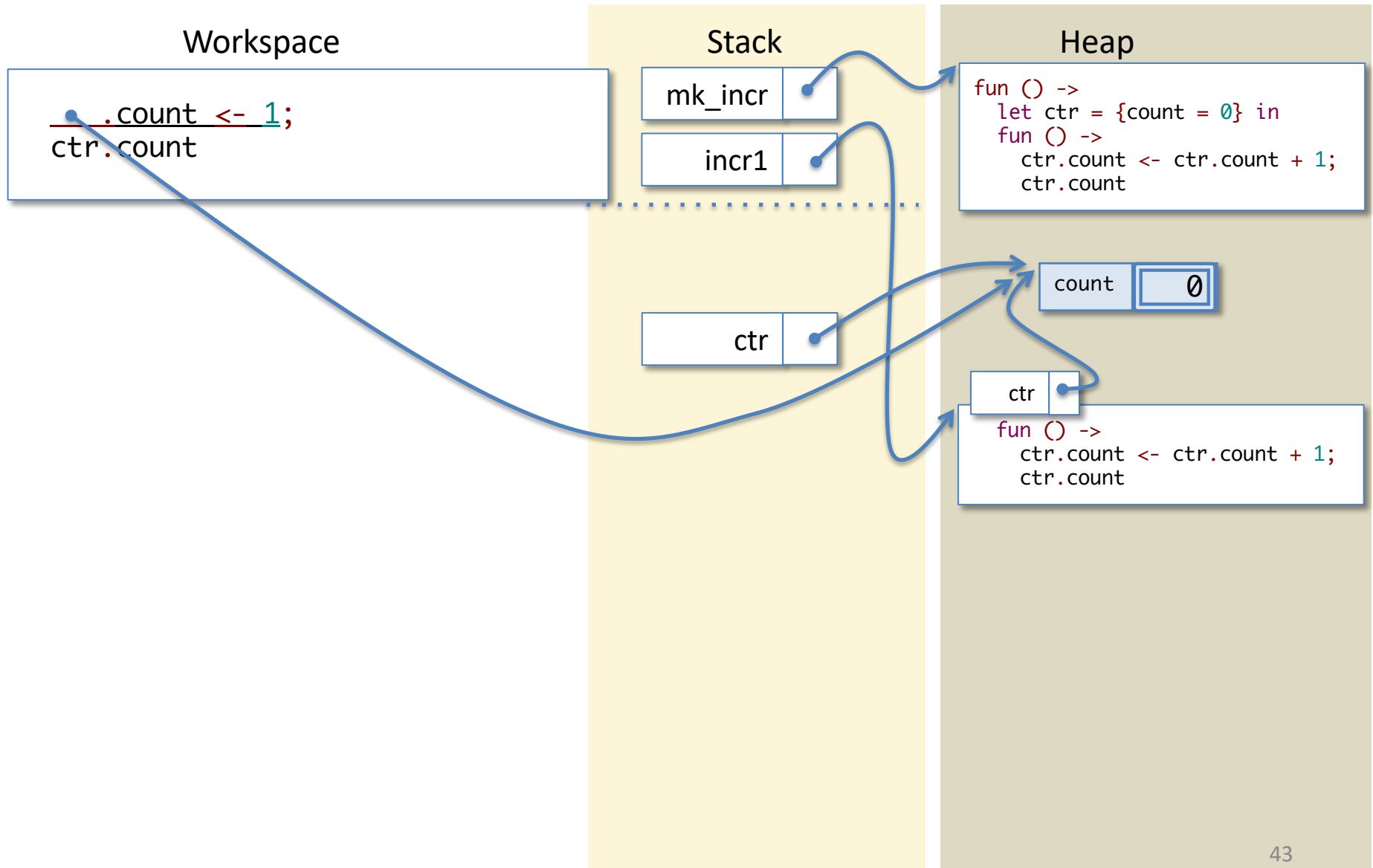
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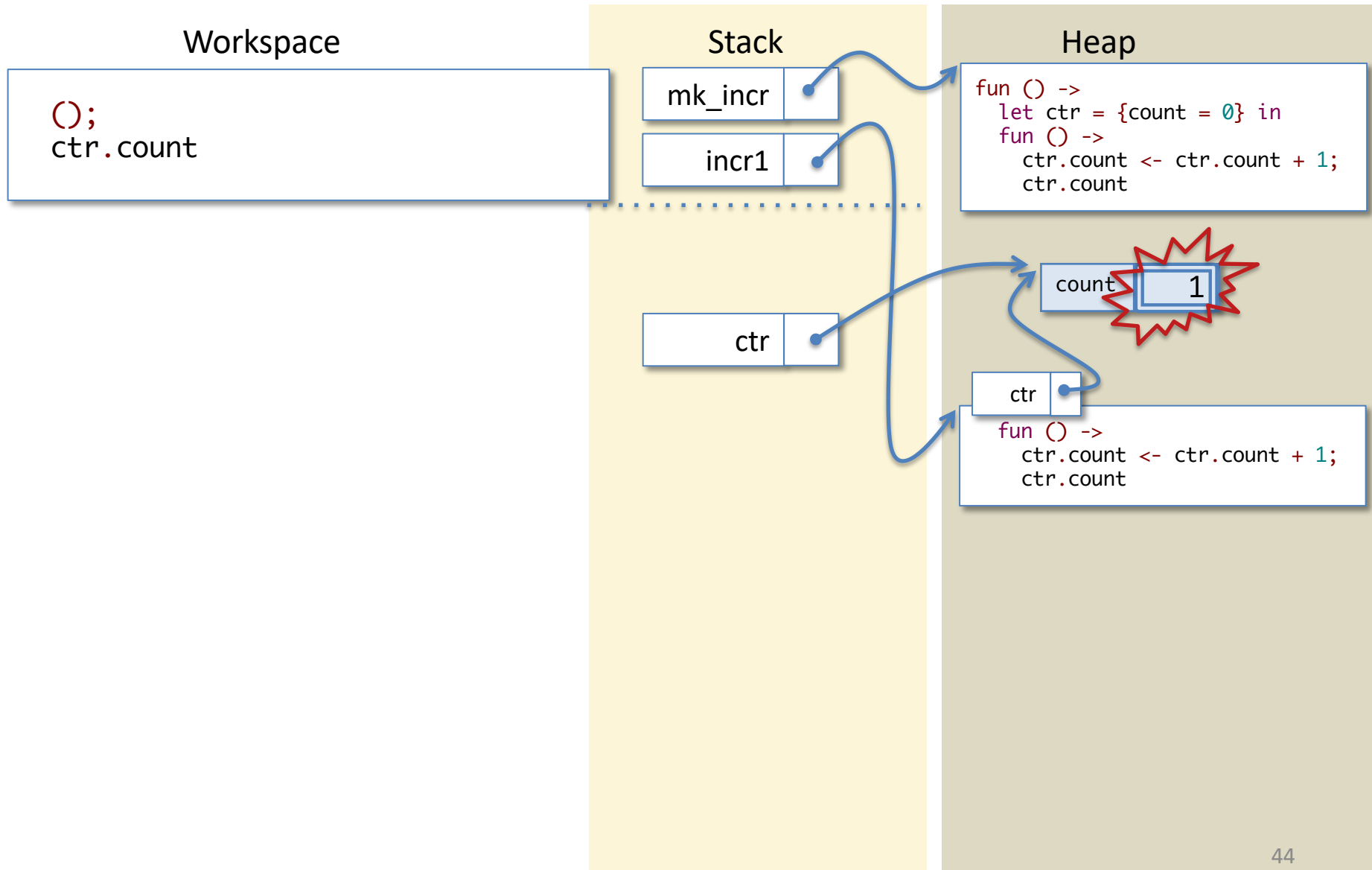
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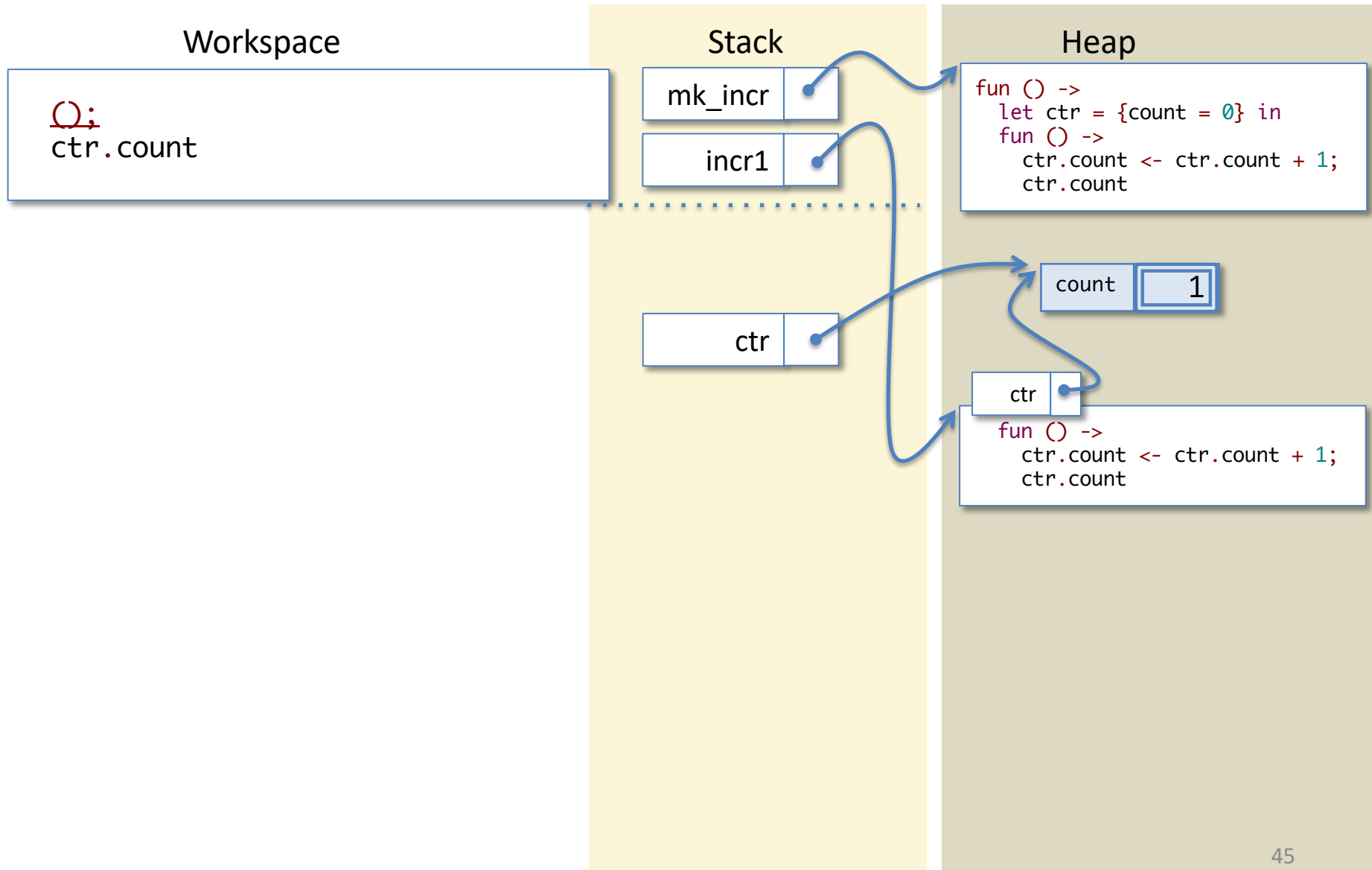
Now let's run "incr1 ()"



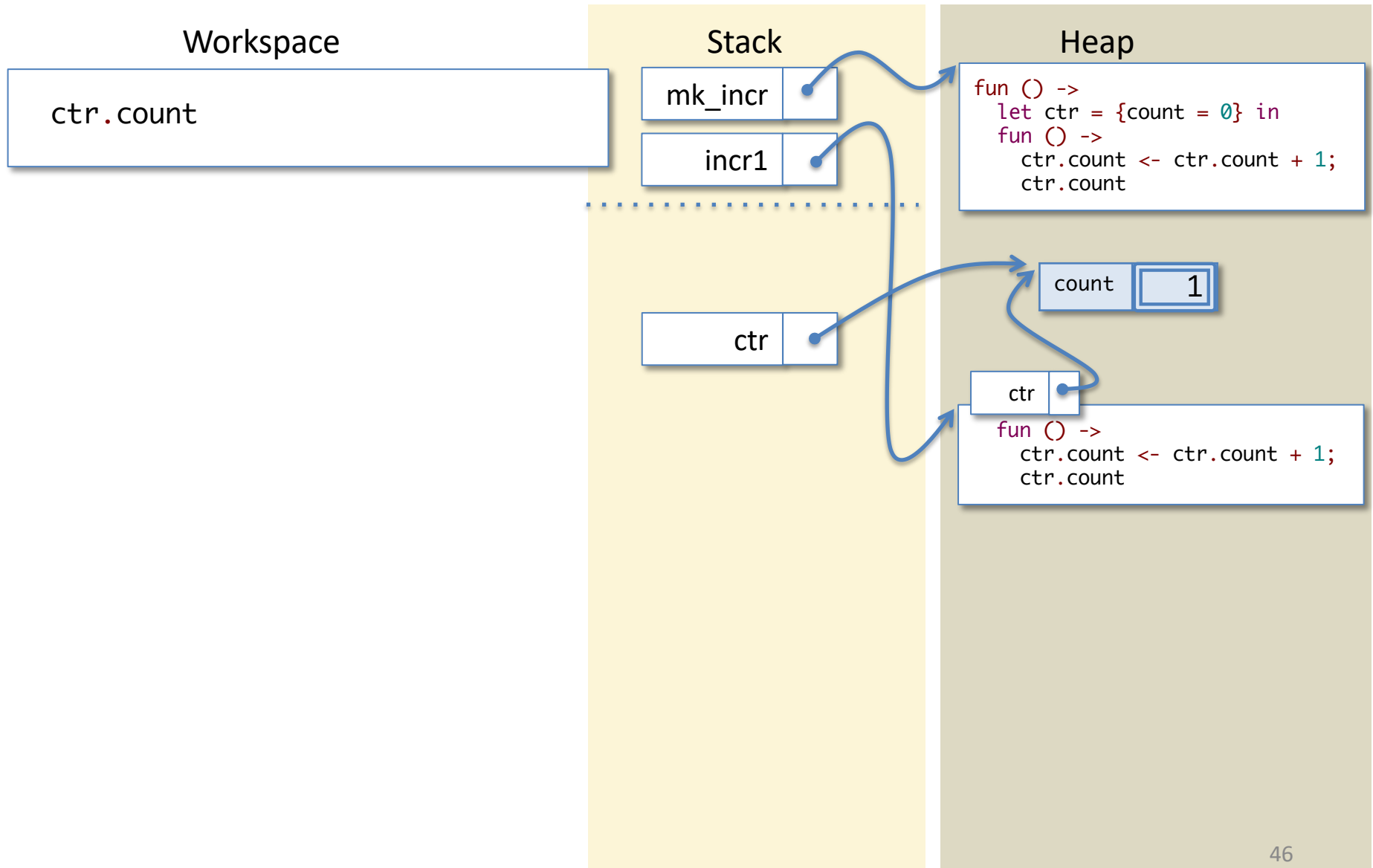
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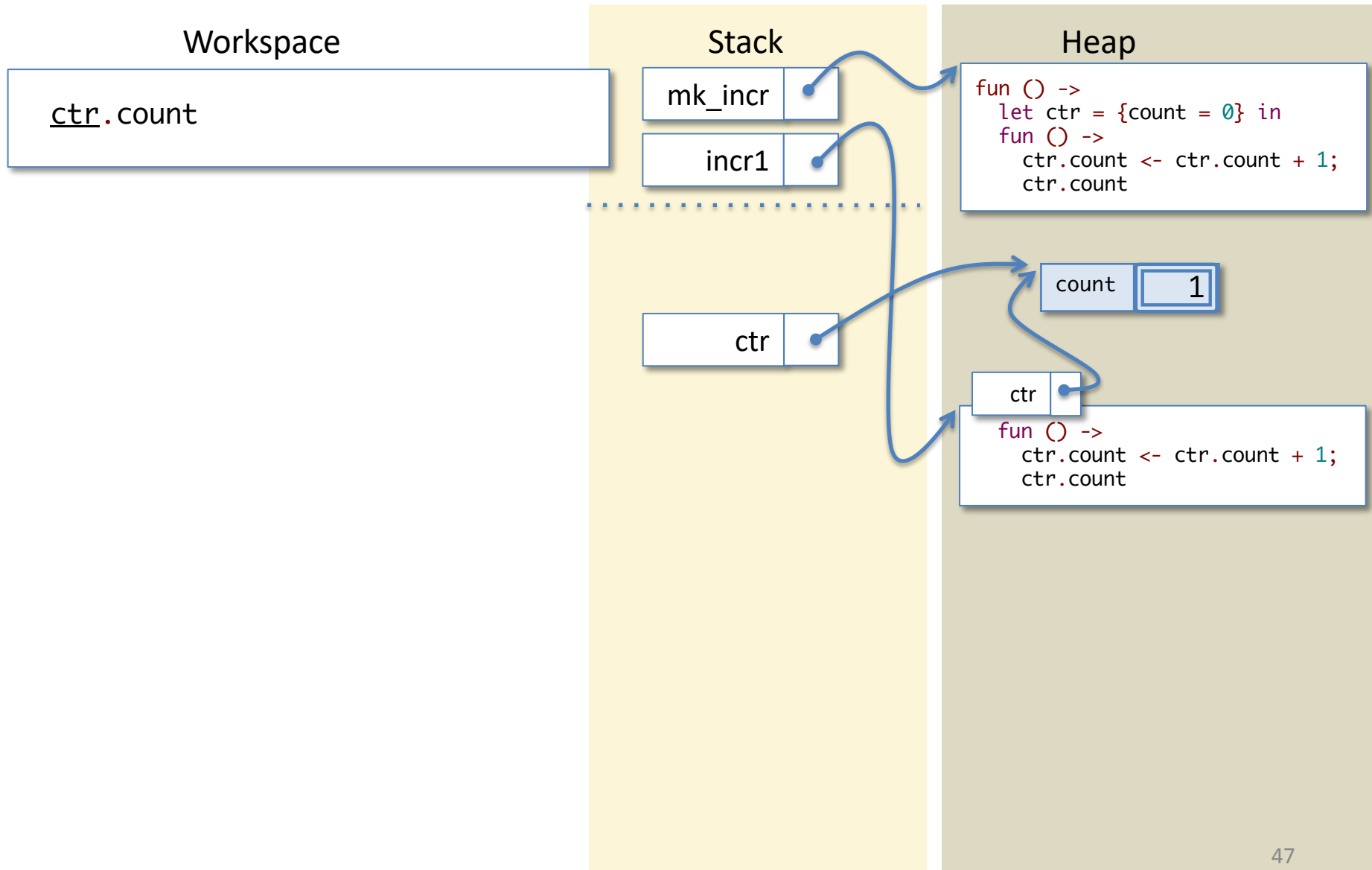
Now let's run "incr1 ()"



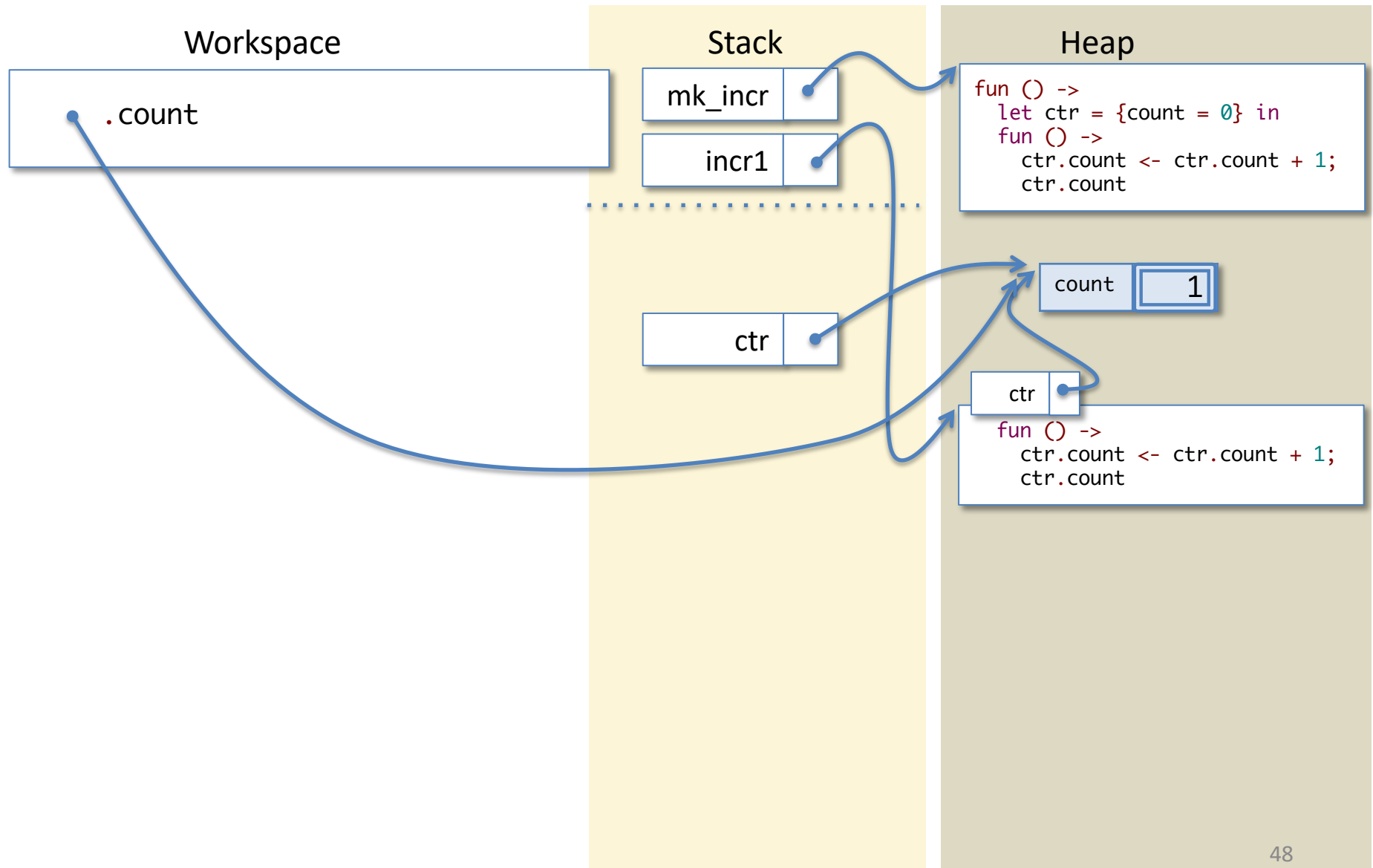
Now let's run "incr1 ()"



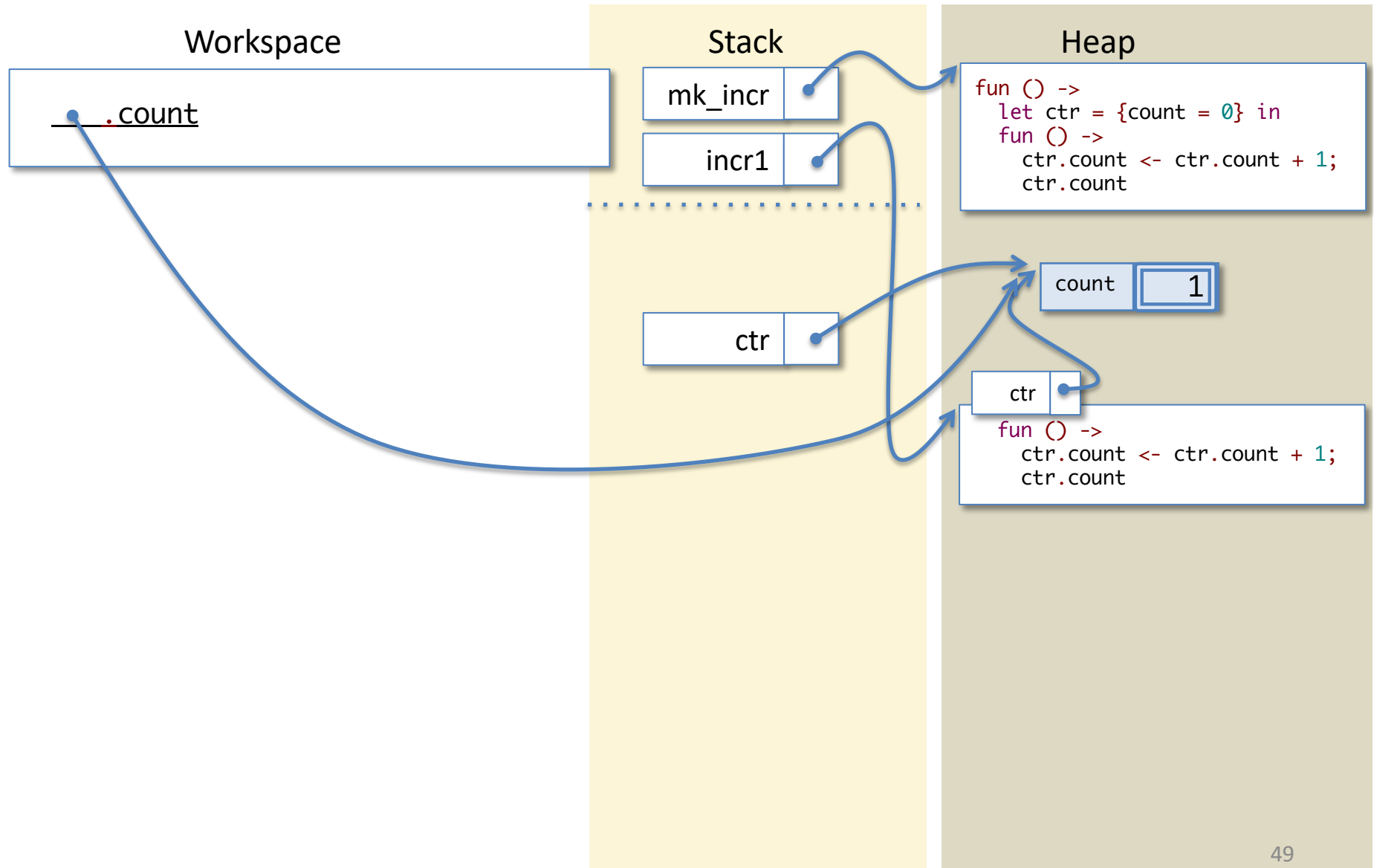
Now let's run "incr1 ()"



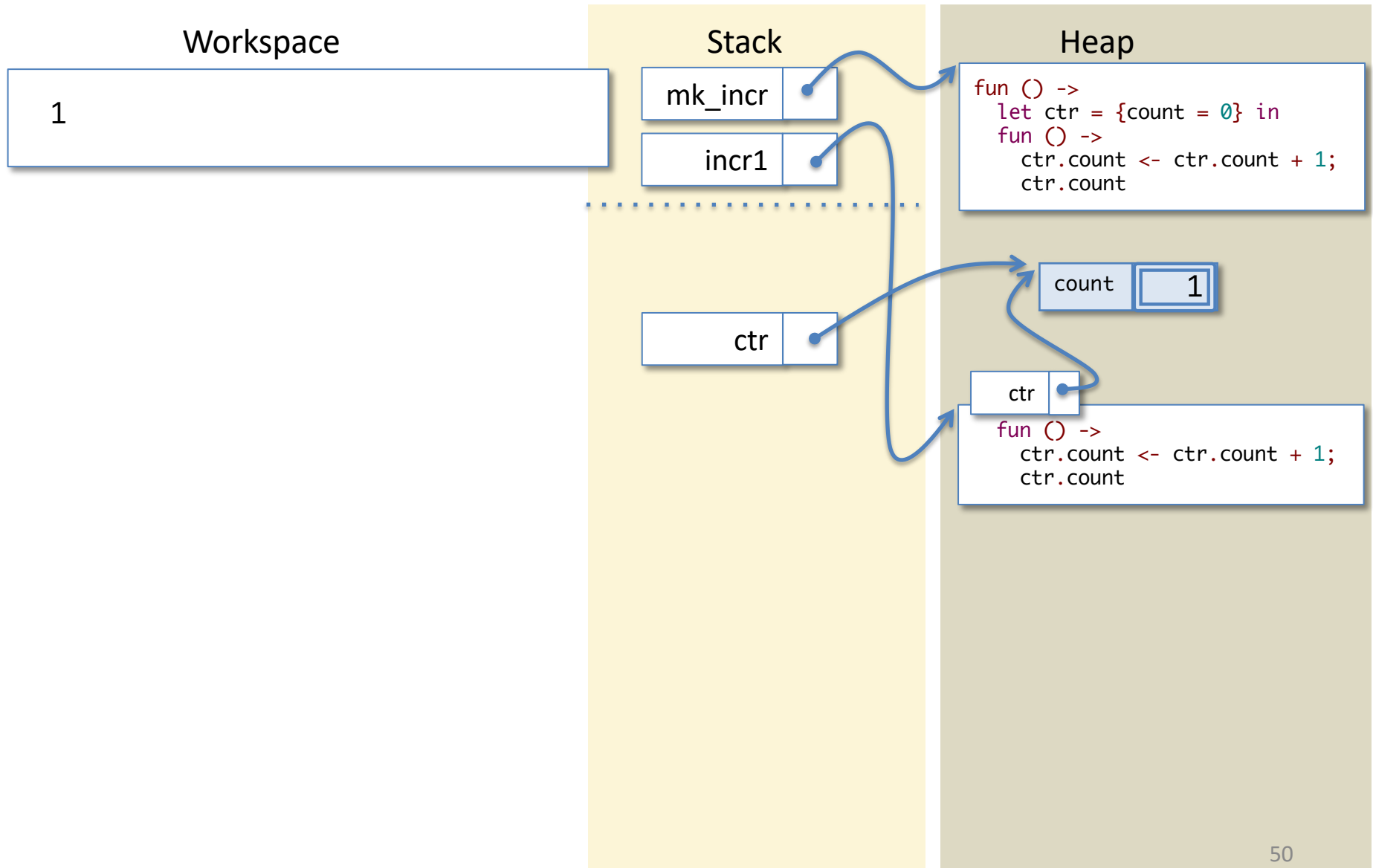
Now let's run "incr1 ()"



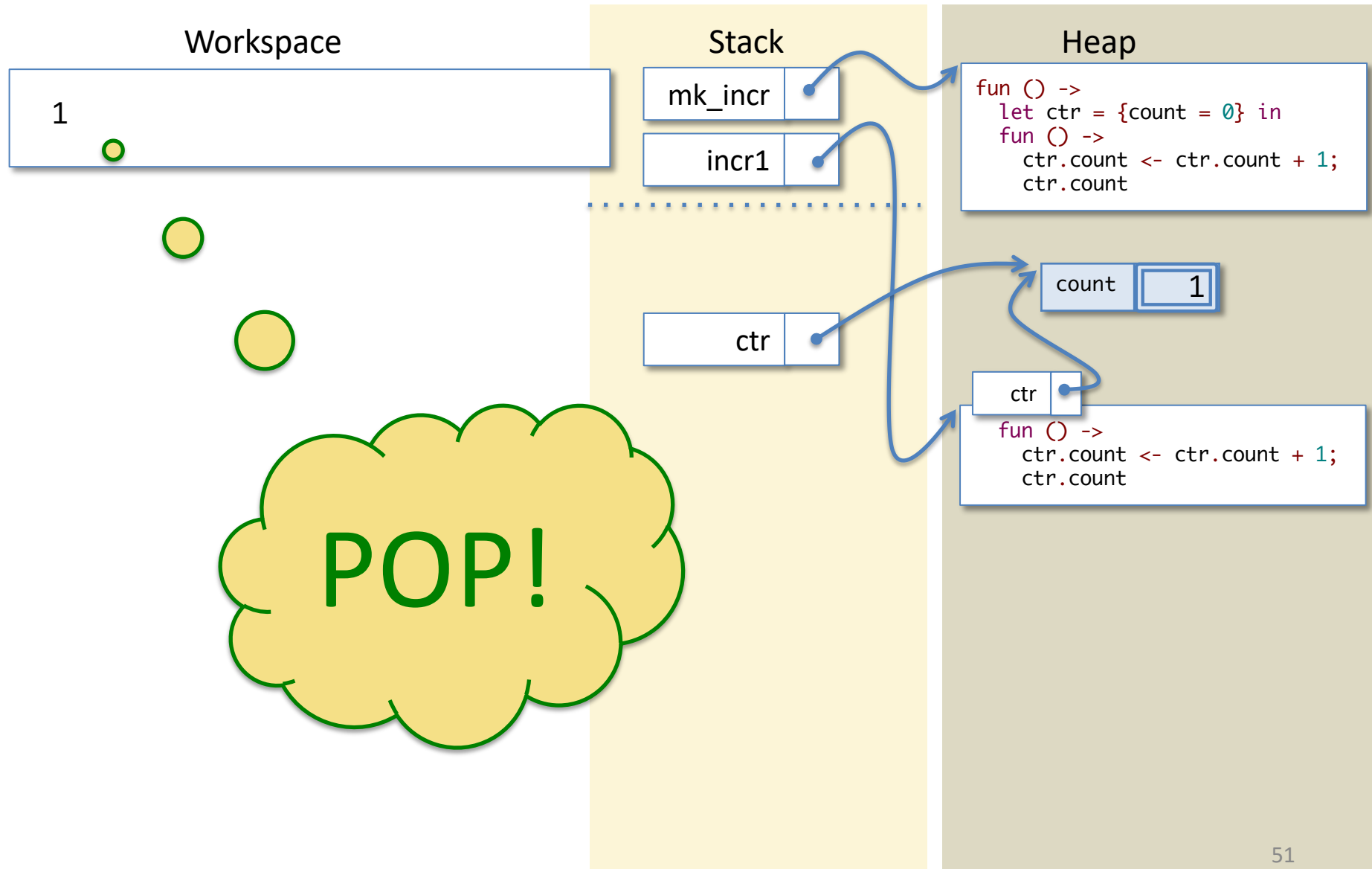
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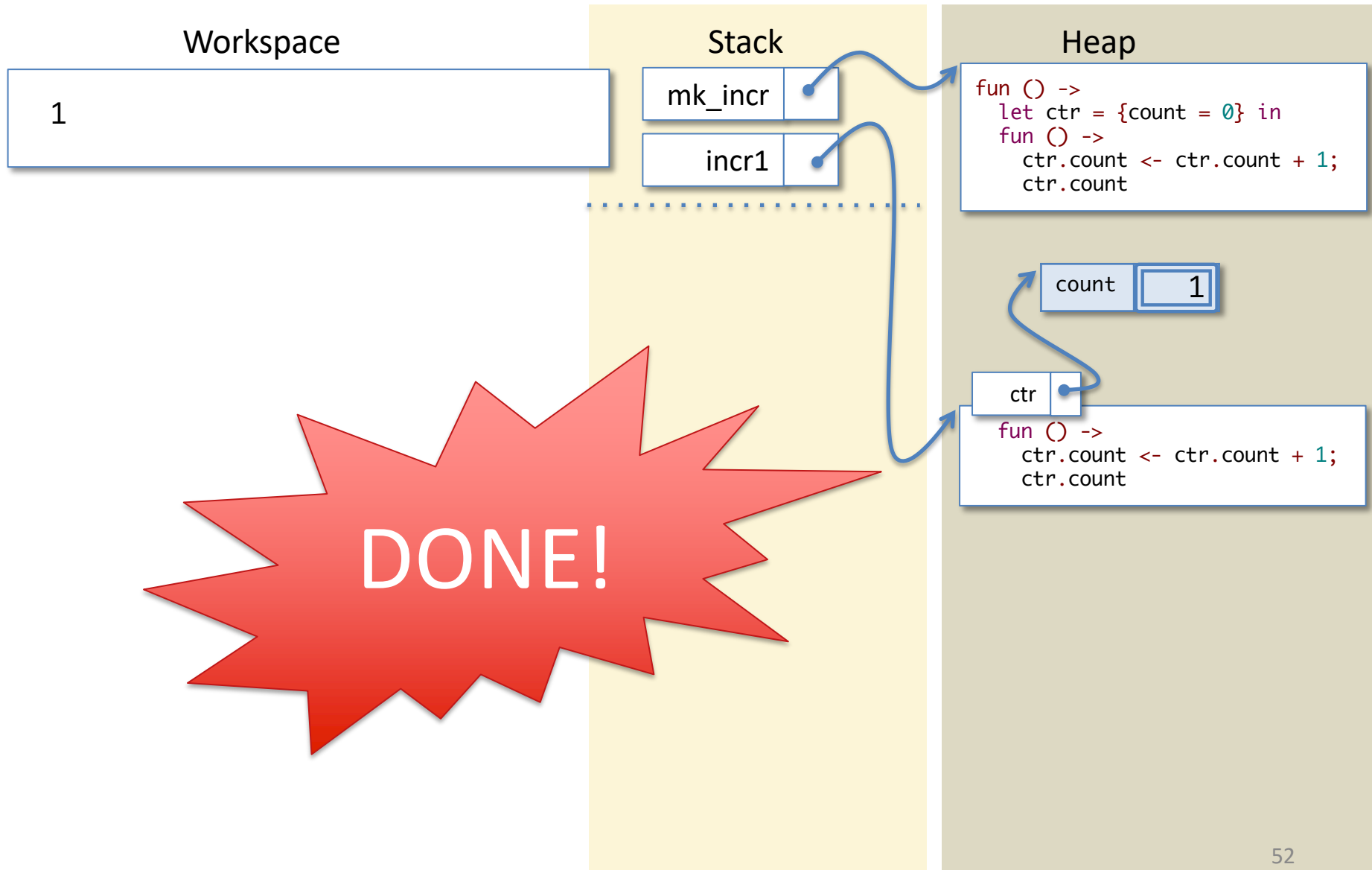
Now let's run "incr1 ()"



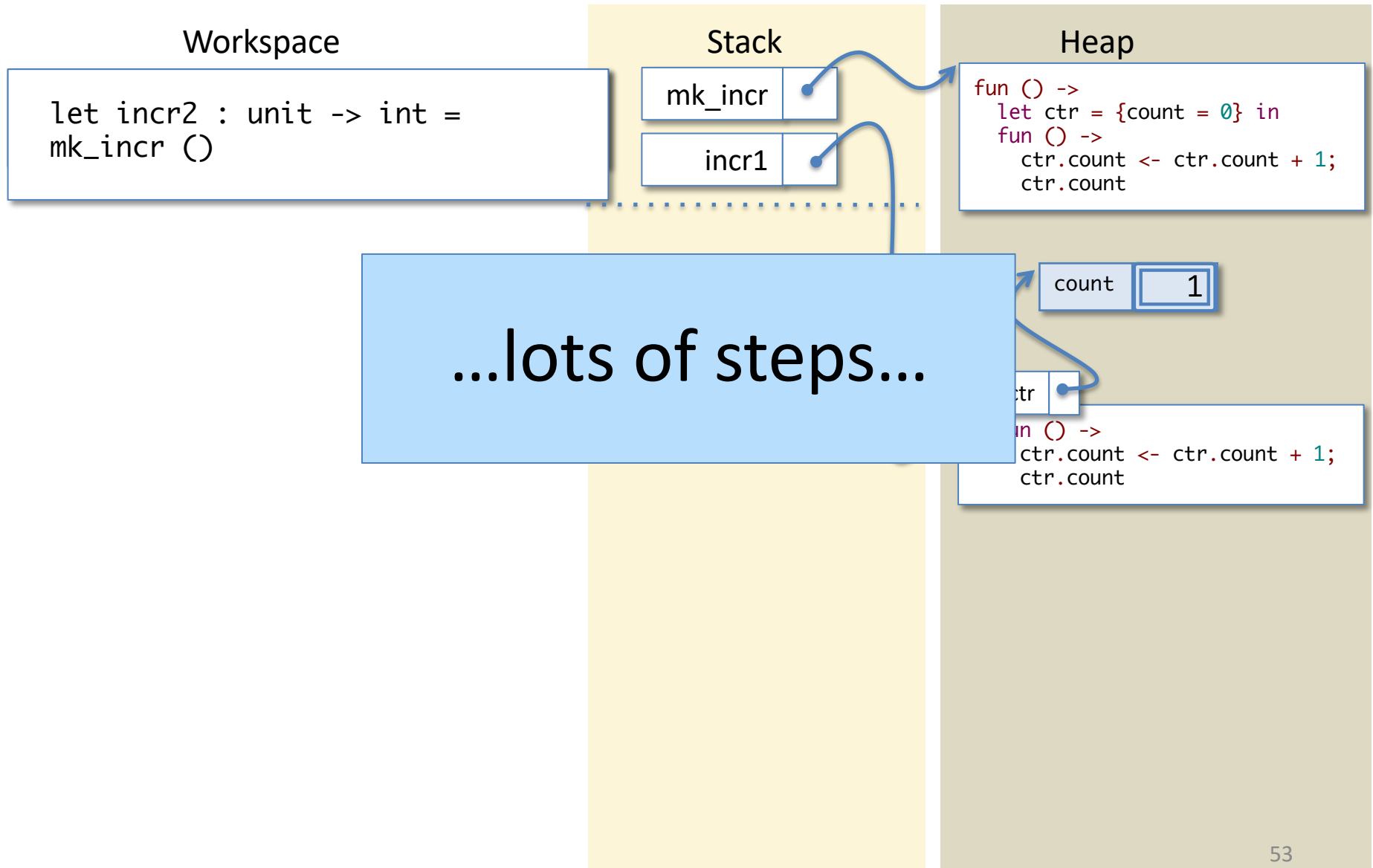
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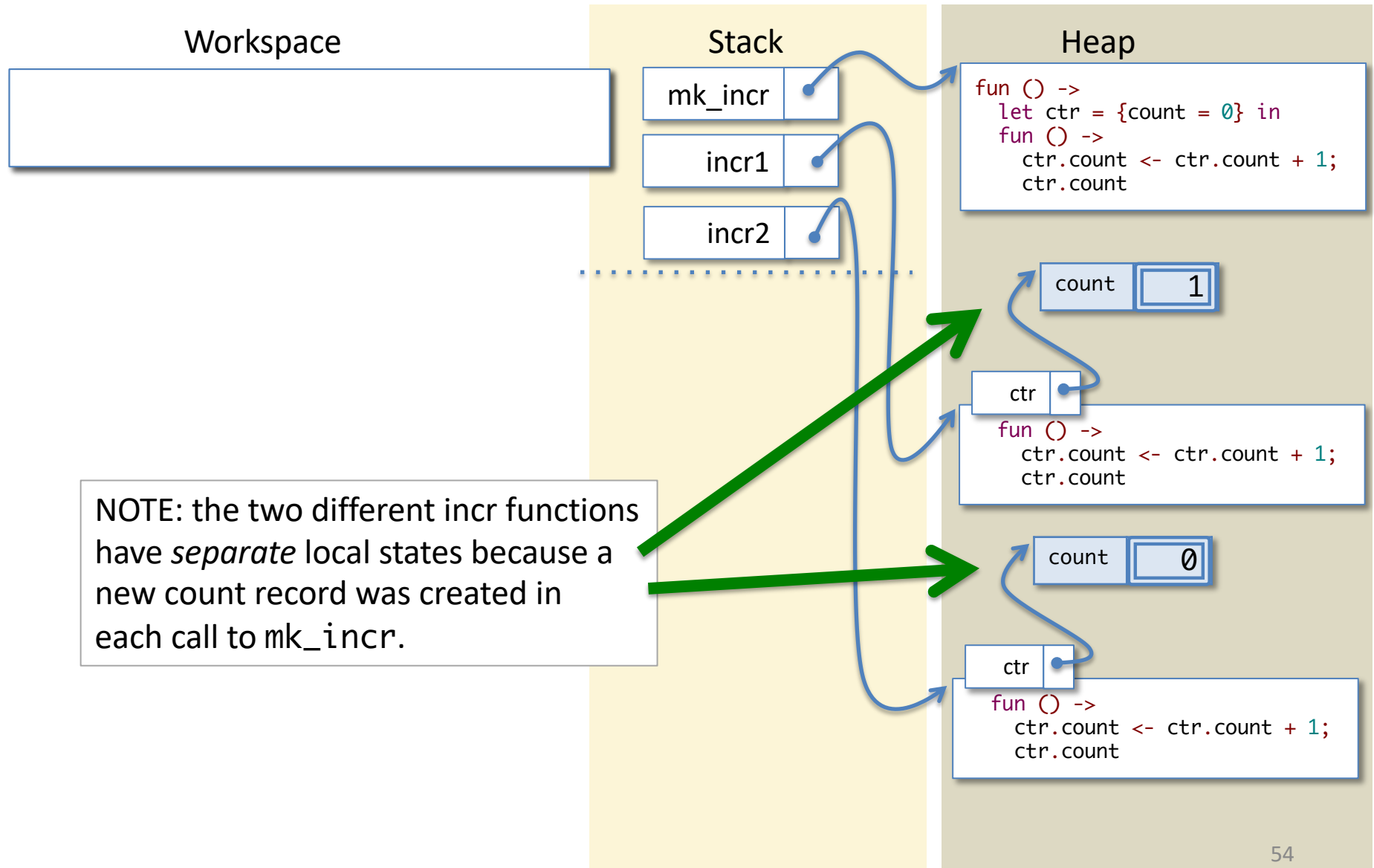
Now let's run "incr1 ()"



Now Let's run `mk_incr` again



After creating incr2...



Objects

One step further...

- `mk_incr` illustrates how to create different instance of local state so that we can make as many counters as we need
- What if we wanted to bundle together *several* operations that share the same local state?
 - e.g. `incr` and `decr` operations that work on the same counter

Key Concept: *Object*

An object consists of:

- some encapsulated mutable state (*fields*)
- a set of operations that manipulate that state (*methods*)

A Counter *Object*

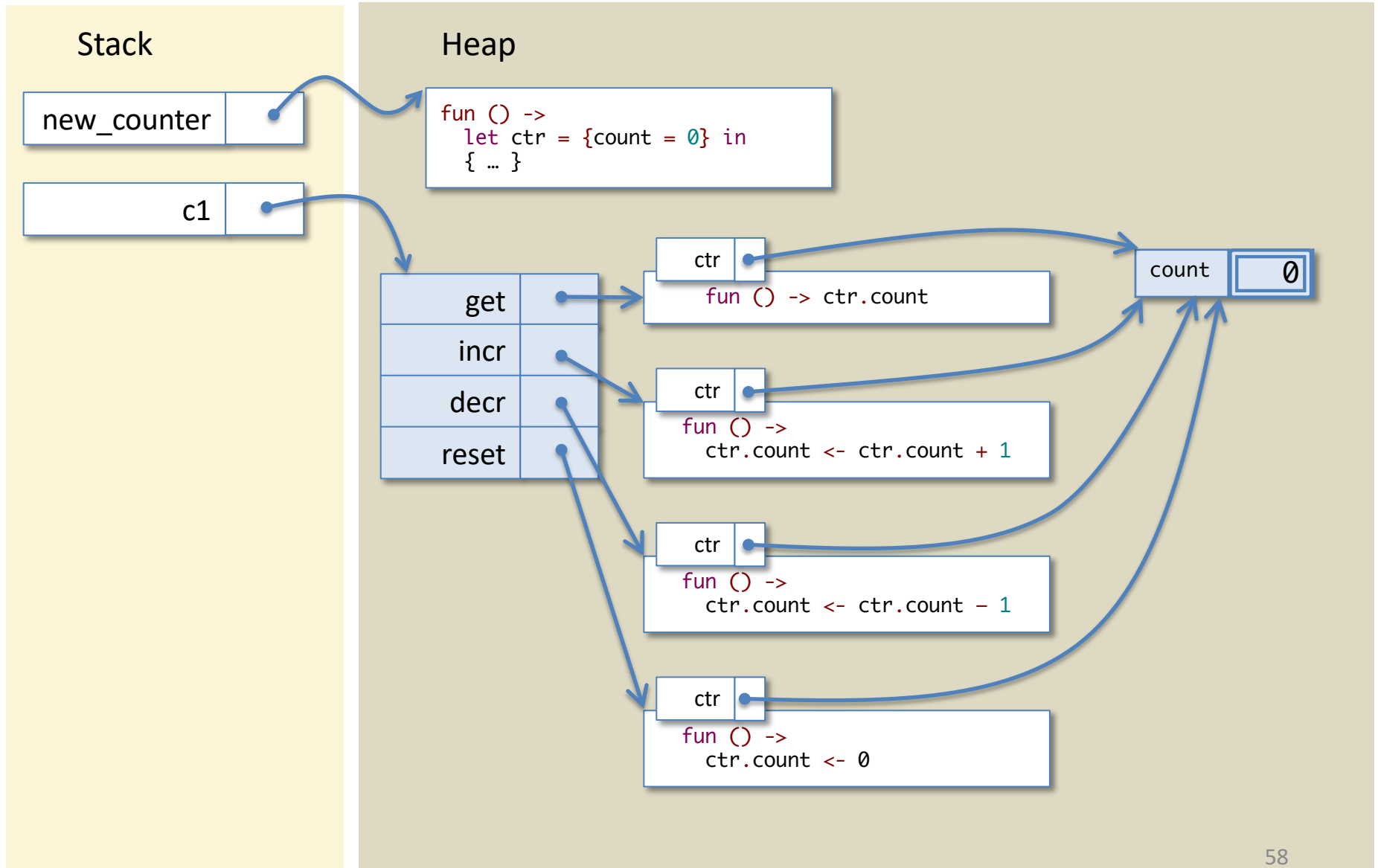
```
(* The type of counter objects *)
```

```
type counter = {  
  get    : unit -> int;  
  incr   : unit -> unit;  
  decr   : unit -> unit;  
  reset  : unit -> unit;  
}
```

```
(* Create a fresh counter object with hidden state: *)
```

```
let new_counter () : counter =  
  let ctr = {count = 0} in  
  {  
    get    = (fun () -> ctr.count) ;  
    incr   = (fun () -> ctr.count <- ctr.count + 1) ;  
    decr   = (fun () -> ctr.count <- ctr.count - 1) ;  
    reset  = (fun () -> ctr.count <- 0) ;  
  }
```

let c1 = new_counter ()



Using Counter Objects

```
(* a helper function to create a nice string for printing *)
let ctr_string (s:string) (i:int) =
  s ^ ".ctr = " ^ (string_of_int i) ^ "\n"

let c1 = new_counter ()
let c2 = new_counter ()

;; print_string (ctr_string "c1" (c1.get ()))
;; c1.incr ()
;; c1.incr ()
;; print_string (ctr_string "c1" (c1.get ()))
;; c1.decr ()
;; print_string (ctr_string "c1" (c1.get ()))
;; c2.incr ()
;; print_string (ctr_string "c2" (c2.get ()))
;; c2.decr ()
;; print_string (ctr_string "c2" (c2.get ()))
```

Typechecking Revisited

How does OCaml* typecheck your code?

*Historical aside: the algorithm we are about to see is known as the Damas-Hindley-Milner type inference algorithm. Turing Award winner Robin Milner was, among other things, the inventor of "ML" (for "meta language"), from which OCaml gets its "ml".

OCaml Typechecking Errors

```
115 let length (q: 'a queue) : int =
116     let rec loop (qn : 'a qnode option) (acc: int) : int
117         |>
118         | None -> []
119         | Some n -> loop n.next (1 + acc)
120
121 in
122 let
```

✖ This expression has type 'a list
but an expression was expected of type int

```
type ('k,'v) map = ('k * 'v) list
```

```
(* A finite map that contains no entries. *)
```

```
let empty () = []
```

```
let rec mem
```

```
begin ma
```

```
| [] ->
```

```
| (k,v):
```

```
if key
```

```
(key = k) || (mem key rest)
```

```
end
```

```
;; run_test "mem test" (fun () ->
```

```
mem "b" [("a",3); ("b",4)]
```

```
)
```

✖ Signature mismatch:

...

Values do not match:

val empty : unit -> 'a list

is not included in

val empty : ('k, 'v) map

File "finiteMap.ml", line 13, characters 2-27: Expected

declaration

File "finiteMap.ml", line 60, characters 6-11: Actual declaration

Typechecking

How do you determine the type of an expression?

1. Recursively determine the types of *all* of the sub-expressions

– Some expressions have “obvious” types:

3 : int “foo” : string true : bool

– Identifiers have the types assigned where they are bound

- Let and function arguments have type annotations
- Or, take the types from the module signature

2. Expressions that *construct* structured values have compound types built from the types of sub-expressions:

(3, “foo”) : int * string
(fun (x:int) -> x + 1) : int -> int
Node(Empty, (3, “foo”), Empty) : (int * string) tree

Typechecking II

3. The type of a function-application expression is obtained as the result from the function type:

- Given an expression of function type $f : T_1 \rightarrow T_2$
- and an argument expression $e : T_1$ (of the input type)
- $(f e) : T_2$

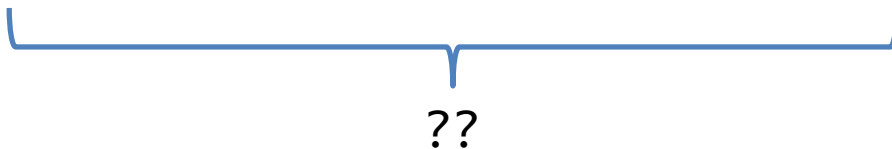
`((fun (x:int) (y:bool) -> y) 3) : ??`

Typechecking II

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- Given a function $f : T_1 \rightarrow T_2$
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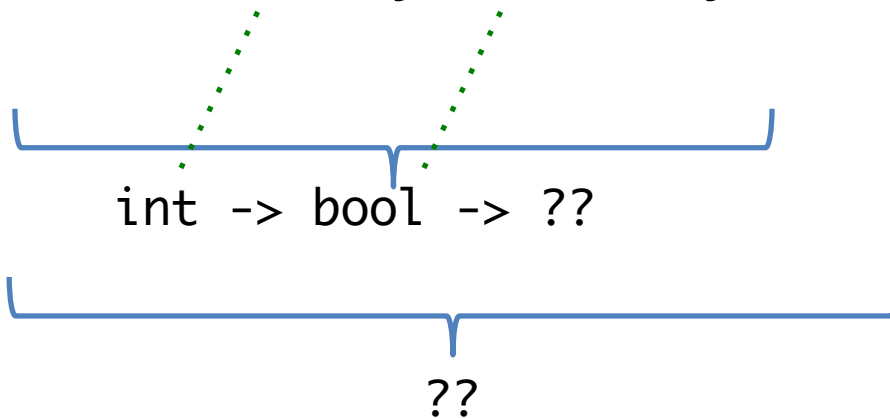
??

Typechecking II

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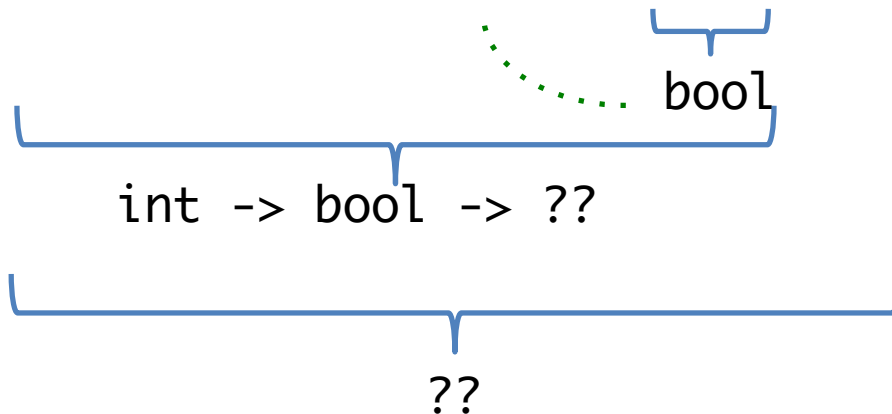


Typechecking II

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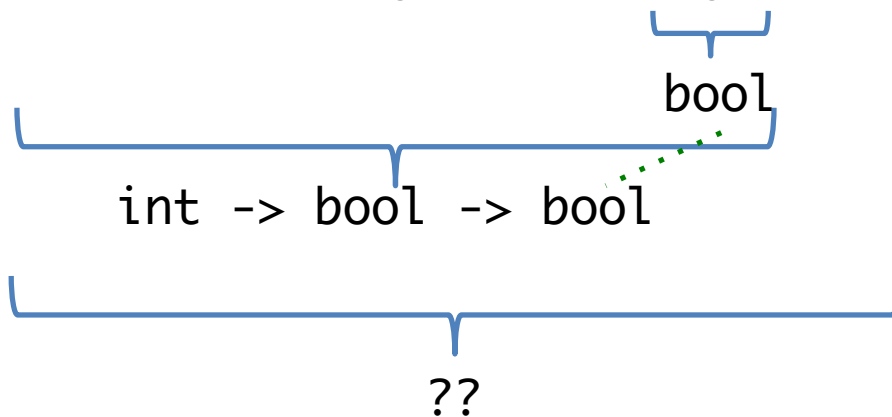


Typechecking II

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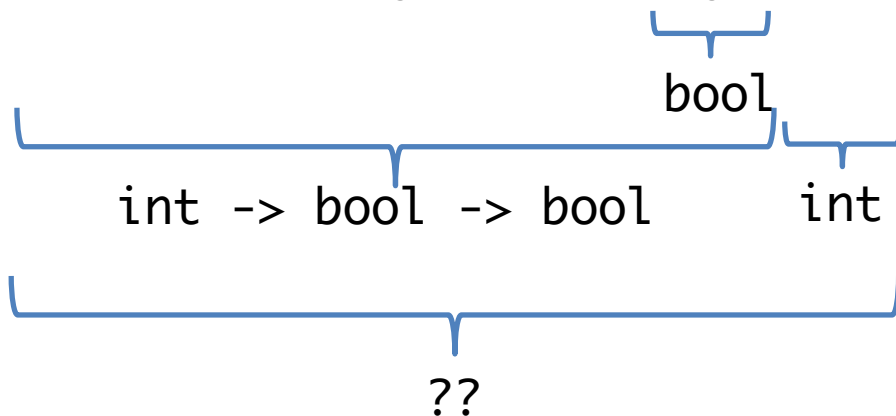


Typechecking II

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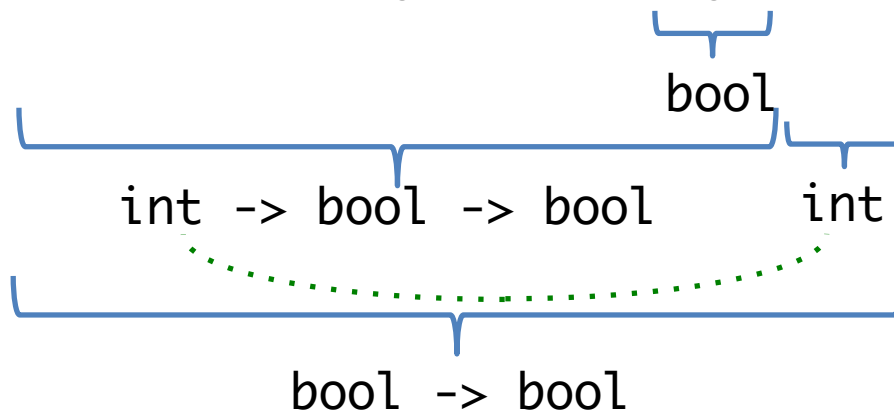


Typechecking II

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- and an argument $e : T_1$ of the input type
- $(f e) : T_2$

`((fun (x:int) (y:bool) -> y) 3) : ??`



Here:

$T_1 = \text{int}$

$T_2 = \text{bool} \rightarrow \text{bool}$

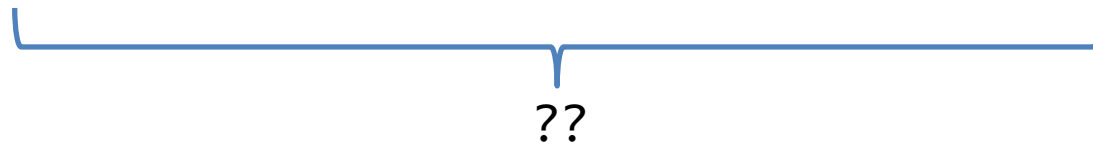
Typechecking III

- For generic expressions:
 - *Unify* the types based on use:
 - Given a function $f : T_1 \rightarrow T_2$
 - and an argument $e : U_1$ of the input type
 - “*match up*” T_1 and U_1 to obtain information about type parameters in T_1 and U_1 based on their usage
 - Obtain an *instantiation*: e.g. ‘ $a = \text{int list}$ ’
 - *Propagate* that information to all occurrences of ‘ a ’

Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

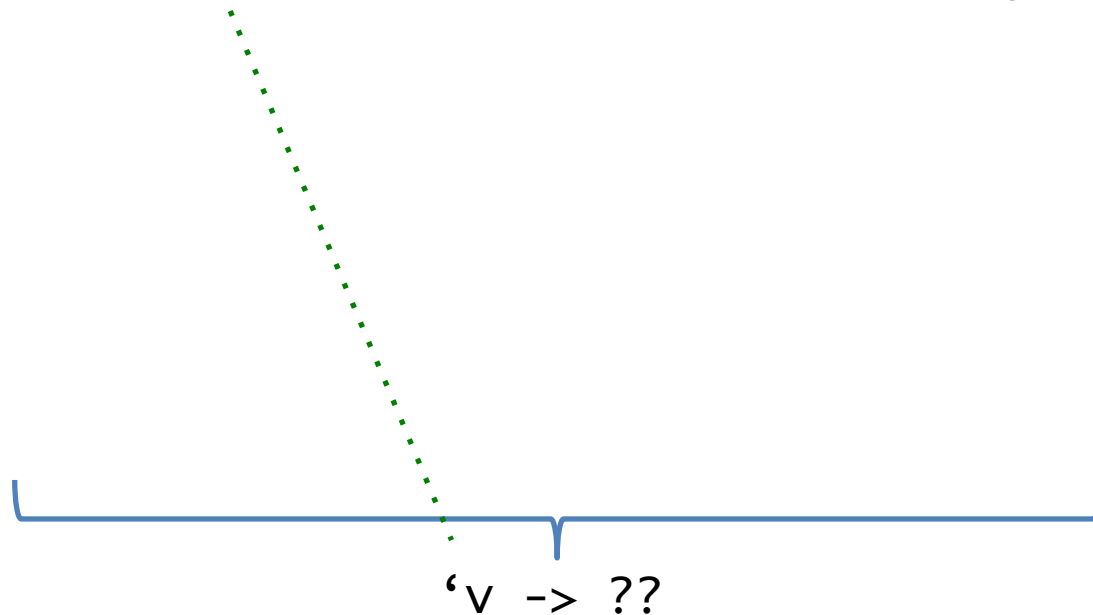


??

Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

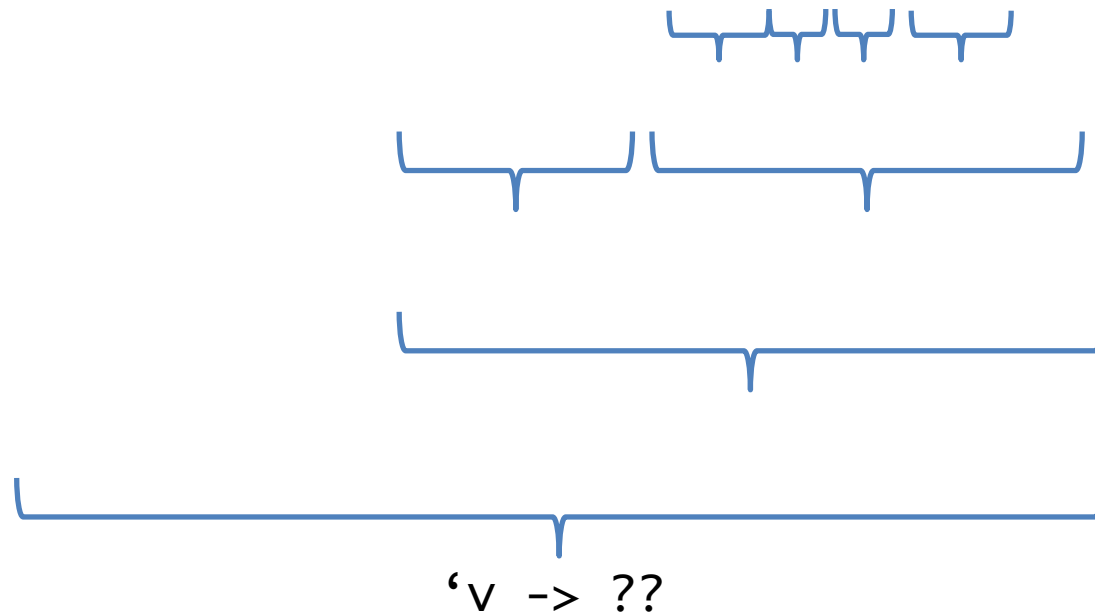
```
fun (x:'v) -> entries (add 3 x empty)
```



Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```



Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

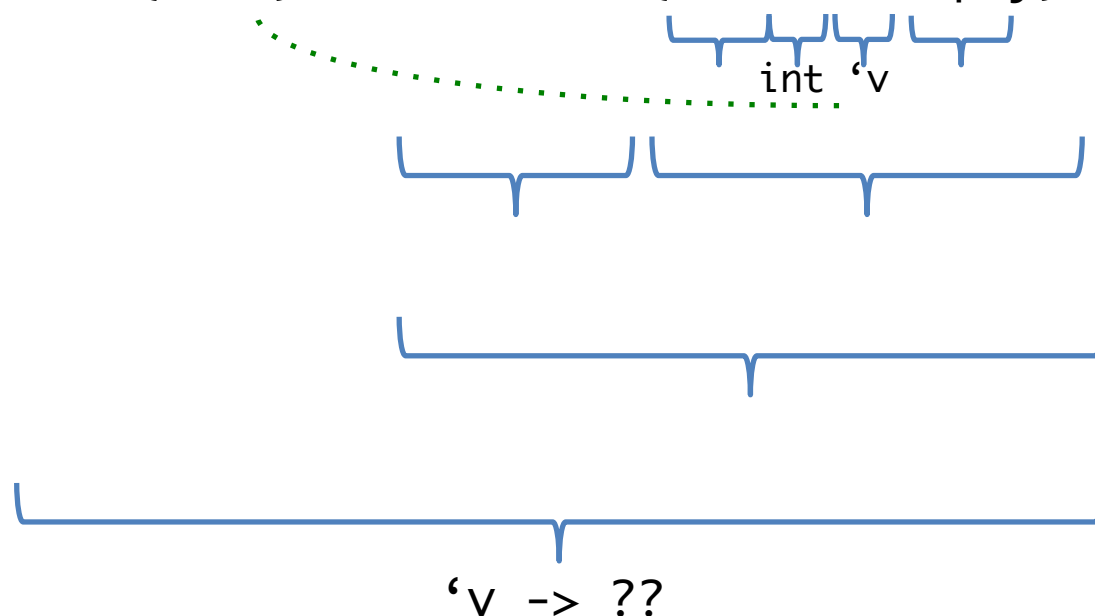


`'v -> ??`

Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```



Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

int 'v ('k, 'v) map

'v -> ??

Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

int 'v ('k, 'v) map

'v -> ??

Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

int 'v ('k, 'v) map

??

'v -> ??

Example Typechecking Problem

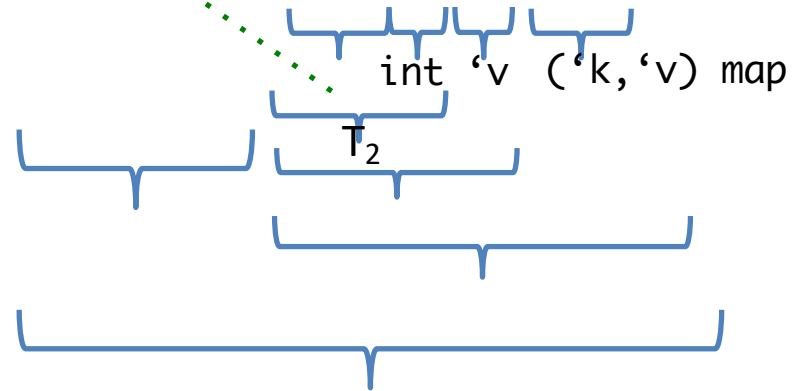
```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

```
fun (x:'v) -> entries (add 3 x empty)
```

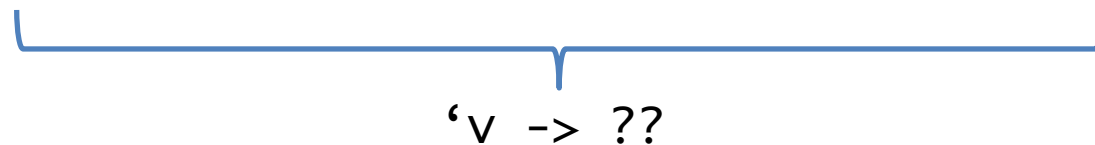
Application:

$T_1 = 'k$

$T_2 = 'v \rightarrow ('k, 'v) \text{ map} \rightarrow ('k, 'v) \text{ map}$



Instantiate: $'k = \text{int}$



Example Typechecking Problem

```

empty   : ('k, 'v) map
add     : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map
entries : ('k, 'v) map -> ('k * 'v) list
  
```

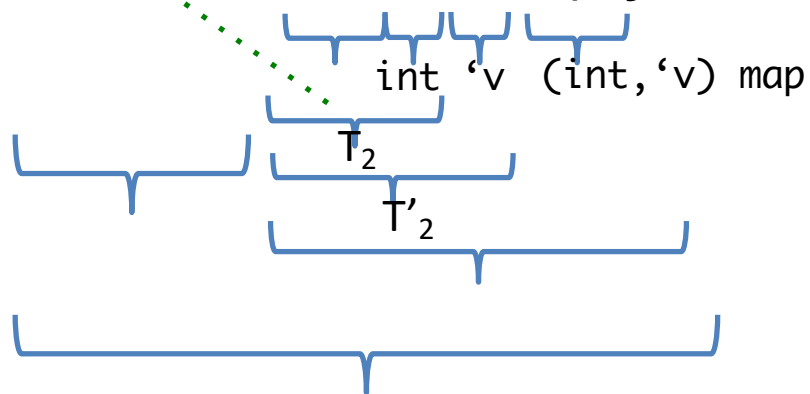
```

fun (x:'v) -> entries (add 3 x empty)
  
```

Another Application:

$T'_1 = 'v$

$T'_2 = (int, 'v) \text{ map} \rightarrow (int, 'v) \text{ map}$



Instantiate: $'v = 'v$

`'v -> ??`

Example Typechecking Problem

```

empty   : ('k, 'v) map
add     : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map
entries : ('k, 'v) map -> ('k * 'v) list
  
```

```

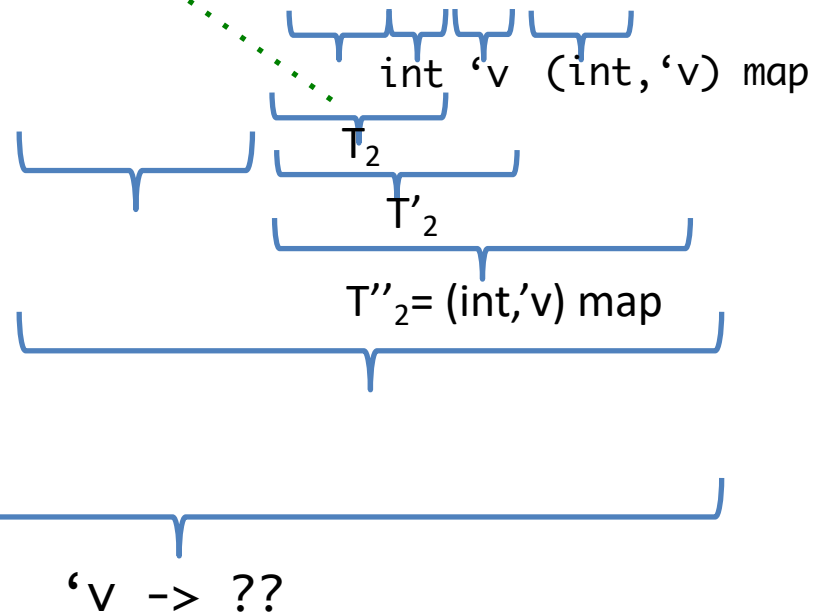
fun (x:'v) -> entries (add 3 x empty)
  
```

A third Application:

$T''_1 = (\text{int}, 'v) \text{ map}$

$T''_2 = (\text{int}, 'v) \text{ map}$

Argument and argument
type already agree



Example Typechecking Problem

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

`fun (x:'v) -> entries (add 3 x empty)`

$U_1 \rightarrow U_2$

T_2

T'_2

$T''_2 = (\text{int}, 'v) \text{ map}$

$'v \rightarrow ??$

Example Typechecking Problem

```

empty   : ('k, 'v) map
add     : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map
entries : ('k, 'v) map -> ('k * 'v) list
    
```

fun (x:'v) -> entries (add 3 x empty)

Another Application:

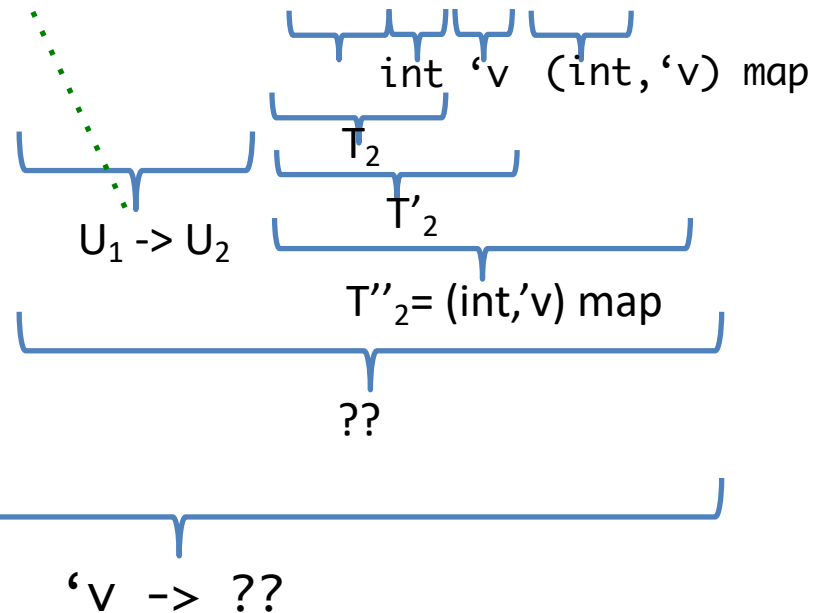
$U_1 = ('k, 'v) \text{ map}$

$U_2 = ('k * 'v) \text{ list}$

Unify U_1 with T''_2

$('k, 'v) \text{ map} \sim\sim (\text{int}, 'v) \text{ map}$

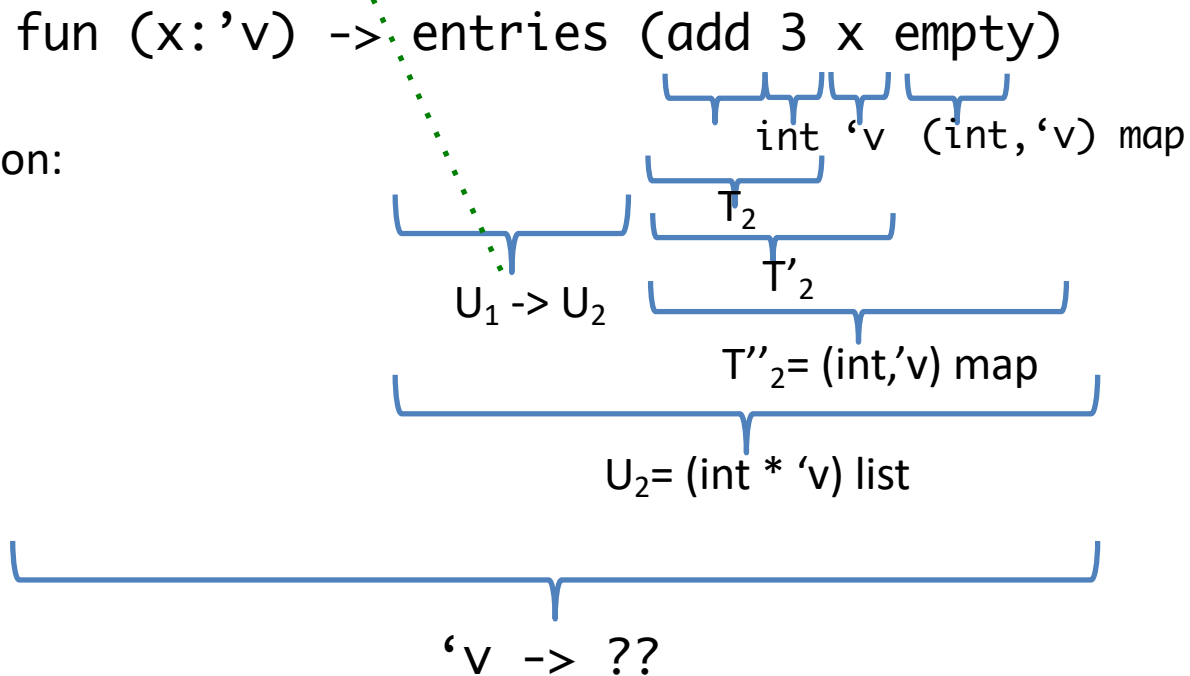
Instantiate $'k = \text{int}$



Example Typechecking Problem

```

empty   : ('k, 'v) map
add     : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map
entries : ('k, 'v) map -> ('k * 'v) list
    
```



Another Application:

$U_1 = (int, 'v) map$

$U_2 = (int * 'v) list$

Example Typechecking Problem

```

empty    : ('k, 'v) map
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map
entries  : ('k, 'v) map -> ('k * 'v) list
    
```

fun (x:'v) -> entries (add 3 x empty)

int 'v ('k, 'v) map

$U_1 \rightarrow U_2$

T_2

T'_2

$T''_2 = ('k, 'v) \text{ map}$

$U_2 = (\text{int} * 'v) \text{ list}$

$'v \rightarrow (\text{int} * 'v) \text{ list}$

Another Application:

$U_1 = (\text{int}, 'v) \text{ map}$

$U_2 = (\text{int} * 'v) \text{ list}$

Ill-typed Expressions?

- An expression is ill-typed if, during this type checking process, inconsistent constraints are encountered:

```
empty    : ('k, 'v) map  
add      : 'k -> 'v -> ('k, 'v) map -> ('k, 'v) map  
entries  : ('k, 'v) map -> ('k * 'v) list
```

add 3 true (add "foo" false empty)

Error: found `int` but expected `string`