CIS 500

Software Foundations

Fall 2004

8 November

Announcements

- Midterm II is one week from Wednesday.
- Give Midterm I regrades (problem 8(b)) to Cheryl by November 15.
- Homework 7 due today.
- Homework 8 out today, due November 15.

Exceptions (Chapter 14)

Motivation

Most programming languages provide some mechanism for interrupting the normal flow of control in a program to signal some exceptional condition.

Examples?

> Note that it is always possible to program without exceptions — instead of raising an exception, we return `None`; instead of returning result `x` normally, we return `Some(x)`. But now we need to wrap every function application in a `case` to find out whether it returned a result or an exception.
>
> $\longrightarrow$ much more convenient to build this mechanism into the language.

Varieties of non-local control

There are many ways of adding "non-local control flow"

- `exit(1)`
- `goto`
- `setjmp/longjmp`
- `raise/try` (or `catch/throw`) in many variations
- `callcc` / continuations
- more esoteric variants (cf. many Scheme papers)

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Let's begin with the simplest of these.

An "abort" primitive in STLC

First step: raising exceptions (but not catching them).

`t`	::=	...	*terms*
		`error`	*run-time error*

Evaluation

$$\texttt{error}\ \texttt{t}_2 \longrightarrow \texttt{error} \qquad \text{(E-AppErr1)}$$

$$\texttt{v}_1\ \texttt{error} \longrightarrow \texttt{error} \qquad \text{(E-AppErr2)}$$

- What if we had booleans and numbers in the language?

Typing

Typing

$$\Gamma \vdash \texttt{error} : \texttt{T} \qquad \text{(T-Error)}$$

Typing errors

Note that the typing rule for `error` allows us to give it any type `T`.

$$\Gamma \vdash \texttt{error} : \texttt{T} \qquad \text{(T-Error)}$$

This means that both

```
if x>0 then 5 else error
```

and

```
if x>0 then true else error
```

will typecheck.

Aside: Syntax-directedness

Note that this rule

$$\Gamma \vdash \texttt{error} : \texttt{T} \qquad \text{(T-Error)}$$

has a problem from the point of view of implementation: it is not syntax-directed!

This will cause the Uniqueness of Types theorem to fail.

For purposes of defining the language and proving its type safety, this is not a problem — Uniqueness of Types is not critical.

Let's think a little, though, about how the rule might be fixed...

An alternative

Can't we just decorate the `error` keyword with its intended type, as we have done to fix related problems with other constructs?

$$\Gamma \vdash \texttt{(error as T) : T} \qquad \text{(T-Error)}$$

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No, this doesn't work!

E.g. (assuming our language also has numbers and booleans):

```
      succ (if (error as Bool) then 5 else 7)
⟶     succ (error as Bool)
```

Exercise: Come up with a similar example using just functions and `error`.

Another alternative

In a system with universal polymorphism (like OCaml), the variability of typing for `error` can be dealt with by assigning it a variable type!

$$\Gamma \vdash \texttt{error} : \texttt{'a} \qquad \text{(T-Error)}$$

In effect, we are replacing the uniqueness of typing property by a weaker (but still useful) property called most general typing.

I.e., although a term may have many types, we always have a compact way of representing the set of all of its possible types.

Yet another alternative

Alternatively, in a system with subtyping (which we'll discuss in the next lecture) and a minimal `Bot` type, we can give `error` a unique type:

$$\Gamma \vdash \texttt{error} : \texttt{Bot} \qquad \text{(T-Error)}$$

(Of course, what we've really done is just pushed the complexity of the old `error` rule onto the `Bot` type! We'll return to this point later.)

For now...

Let's stick with the original rule

$$\Gamma \vdash \texttt{error} : \texttt{T} \qquad \text{(T-Error)}$$

and live with the resulting nondeterminism of the typing relation.

Type safety

The preservation theorem requires no changes when we add `error`: if a term of type `T` reduces to `error`, that's fine, since `error` has every type `T`.

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Progress, though, requires a litte more care.

Progress

First, note that we do not want to extend the set of values to include `error`, since this would make our new rule for propagating errors through applications.

$$v_1 \ \texttt{error} \longrightarrow \texttt{error} \qquad \text{(E-AppErr2)}$$

overlap with our existing computation rule for applications:

$$(\lambda x{:}T_{11}.t_{12}) \ v_2 \longrightarrow [x \mapsto v_2]t_{12} \qquad \text{(E-AppAbs)}$$

e.g., the term

```
(λx:Nat.0) error
```

could evaluate to either `0` (which would be wrong) or `error` (which is what we intend).

Progress

Instead, we keep `error` as a non-value normal form, and refine the statement of progress to explicitly mention the possibility that terms may evaluate to `error` instead of to a value.

> THEOREM [PROGRESS]: Suppose `t` is a closed, well-typed normal form. Then either `t` is a value or `t` = `error`.

Catching exceptions

$\mathtt{t} \quad ::= \quad \ldots$ *terms*

$\quad\quad \mathtt{try\ t\ with\ t}$ *trap errors*

Evaluation

$$\mathtt{try\ v_1\ with\ t_2} \longrightarrow \mathtt{v_1} \qquad \text{(E-TryV)}$$

$$\mathtt{try\ error\ with\ t_2} \longrightarrow \mathtt{t_2} \qquad \text{(E-TryError)}$$

$$\frac{\mathtt{t_1} \longrightarrow \mathtt{t_1'}}{\mathtt{try\ t_1\ with\ t_2} \longrightarrow \mathtt{try\ t_1'\ with\ t_2}} \qquad \text{(E-Try)}$$

Typing

$$\frac{\Gamma \vdash \mathtt{t_1 : T} \qquad \Gamma \vdash \mathtt{t_2 : T}}{\Gamma \vdash \mathtt{try\ t_1\ with\ t_2 : T}} \qquad \text{(T-Try)}$$

Exceptions carrying values

$\texttt{t} ::= \ldots$ *terms*

$\texttt{raise t}$ *raise exception*

Evaluation

$$\texttt{(raise } v_{11}\texttt{) } t_2 \longrightarrow \texttt{raise } v_{11} \qquad \text{(E-AppRaise1)}$$

$$v_1 \texttt{ (raise } v_{21}\texttt{)} \longrightarrow \texttt{raise } v_{21} \qquad \text{(E-AppRaise2)}$$

$$\frac{t_1 \longrightarrow t_1'}{\texttt{raise } t_1 \longrightarrow \texttt{raise } t_1'} \qquad \text{(E-Raise)}$$

$$\texttt{raise (raise } v_{11}\texttt{)} \longrightarrow \texttt{raise } v_{11} \qquad \text{(E-RaiseRaise)}$$

$$\texttt{try } v_1 \texttt{ with } t_2 \longrightarrow v_1 \qquad \text{(E-TryV)}$$

$$\texttt{try raise } v_{11} \texttt{ with } t_2 \longrightarrow t_2\ v_{11} \qquad \text{(E-TryRaise)}$$

$$\frac{t_1 \longrightarrow t_1'}{\texttt{try } t_1 \texttt{ with } t_2 \longrightarrow \texttt{try } t_1' \texttt{ with } t_2} \qquad \text{(E-Try)}$$

Typing

$$\frac{\Gamma \vdash t_1 : T_{exn}}{\Gamma \vdash \texttt{raise}\ t_1 : T} \qquad \text{(T-Exn)}$$

$$\frac{\Gamma \vdash t_1 : T \qquad \Gamma \vdash t_2 : T_{exn} \to T}{\Gamma \vdash \texttt{try}\ t_1\ \texttt{with}\ t_2 : T} \qquad \text{(T-Try)}$$